Putnam $\Sigma.7$

Po-Shen Loh

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1 Problems

Po-Shen Loh will unfortunately be in Boston during our usual discussion and dinner time. However, you are welcome to come to work on the problems. There will probably be a group doing that anyway.

Putnam 2001/A4. Triangle ABC has area 1. Points E, F, G lie, respectively, on sides BC, CA, AB, such that AE bisects BF at point R, BF bisects CG at point S, and CG bisects AE at point T. Find the area of triangle RST.

Putnam 2001/A5. Prove that there are unique positive integers a, n such that $a^{n+1} - (a+1)^n = 2001$.

Putnam 2001/A6. Can an arc of a parabola inside a circle of radius 1 have a length greater than 4?