Math 301 Homework

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Due 1 December 2017

Complete the following problems. Fully justify each response.

- 1. Complete problems 6, 8, 9, 16, 21 from Applied Combinatorics in Section 6.10.
- 2. A vertex cover in a graph is a set of vertices S such that for every edge $e \in E$, at least one of the endpoints of e is in S.

König's Theorem states the following:

If G is a bipartite graph, then the size of a minimum vertex cover in G is equal to the size of a maximum matching in G.

Show that Hall's Theorem, König's Theorem, and Dilworth's Theorem are equivalent.