

Name: Solution key

Allowed time: 15 mins

1. (4 points) Show that the line of intersection of the planes

$$P_1: x + y - z = 0 \text{ and } P_2: x - y - 5z - 6 = 0$$

is parallel to the line $\mathcal{L}: \frac{x-6}{3} = \frac{-y-3}{2} = \frac{z-3}{2}$.

$$\vec{N}_1 = \langle 1, 1, -1 \rangle, \quad \vec{N}_2 = \langle 1, -1, -5 \rangle$$

$$\vec{N}_1 \times \vec{N}_2 = \begin{vmatrix} \hat{i} & \hat{j} & \hat{k} \\ 1 & 1 & -1 \\ 1 & -1 & -5 \end{vmatrix} = -6\hat{i} + 4\hat{j} - 2\hat{k}$$

parallel vectors.

Direction vector of the line: $\langle 3, -2, 2 \rangle$

2. (4 points) Find the distance from the point
- $A(2, 8, 5)$
- to the plane
- $P: x - 2y - 2z = 1$
- .

$$\text{Distance} = \left| \frac{2 - 2(8) - 2(5) - 1}{\sqrt{1^2 + 2^2 + 2^2}} \right| = \frac{25}{3} \text{ units}$$

3. (2 points) Let
- $\mathbf{g}(t) = 2t\mathbf{i} + t^2\mathbf{j} + \frac{1}{3}t^3\mathbf{k}$
- . Then find the scalar unit tangent vector at the point
- $(6, 9, 9)$
- .

$$\mathbf{g}'(t) = 2\hat{i} + 2t\hat{j} + t^2\hat{k} \quad \text{Note } t = 3$$

$$\text{unit tangent vector at } (6, 9, 9) = \frac{2\hat{i}}{11} + \frac{6\hat{j}}{11} + \frac{9\hat{k}}{11} \quad \underline{\underline{\text{Ans}}}$$

$t = 3$