# Putnam E. 02 

Po-Shen Loh

7 September 2021

## 1 Problems

Putnam 2005/B1. Find a nonzero polynomial $P(x, y)$ such that $P(\lfloor a\rfloor,\lfloor 2 a\rfloor)=0$ for all real numbers $a$. (Note: $\lfloor\nu\rfloor$ is the greatest integer less than or equal to $\nu$.)

Putnam 2005/B2. Find all positive integers $n, k_{1}, \ldots, k_{n}$ such that $k_{1}+\cdots+k_{n}=5 n-4$ and

$$
\frac{1}{k_{1}}+\cdots+\frac{1}{k_{n}}=1
$$

Putnam 2005/B3. Find all differentiable functions $f:(0, \infty) \rightarrow(0, \infty)$ for which there is a positive real number $a$ such that

$$
f^{\prime}\left(\frac{a}{x}\right)=\frac{x}{f(x)}
$$

for all $x>0$.

