Putnam E.03

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15 September 2020

1 Problems

- **Putnam 1988/B1.** A composite (positive integer) is a product ab with a and b not necessarily distinct integers in $\{2, 3, 4, ...\}$. Show that every composite is expressible as xy + xz + yz + 1, with x, y, z positive integers.
- **Putnam 1988/B2.** Prove or disprove: If x and y are real numbers with $y \ge 0$ and $y(y+1) \le (x+1)^2$, then $y(y-1) \le x^2$.
- **Putnam 1988/B3.** For every n in the set $\mathbb{N} = \{1, 2, ...\}$ of positive integers, let r_n be the minimum value of $|c d\sqrt{3}|$ for all nonnegative integers c and d with c + d = n. Find, with proof, the smallest positive real number g with $r_n \leq g$ for all $n \in \mathbb{N}$.