Putnam $\Sigma.12$

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10 November 2019

1 Problems

- **Putnam 1999/B4.** Let f be a real function with a continuous third derivative such that f(x), f'(x), f''(x), f''(x), f'''(x), f''(x), f''(x),
- **Putnam 1999/B5.** For an integer $n \ge 3$, let $\theta = 2\pi/n$. Evaluate the determinant of the $n \times n$ matrix I + A, where I is the $n \times n$ identity matrix and $A = (a_{jk})$ has entries $a_{jk} = \cos(j\theta + k\theta)$ for all j, k.
- **Putnam 1999/B6.** Let S be a finite set of integers, each greater than 1. Suppose that for each integer n there is some $s \in S$ such that gcd(s, n) = 1 or gcd(s, n) = s. Show that there exist $s, t \in S$ such that gcd(s, t) is prime.