

$$M_t = e^{\lambda W_t - \alpha t}$$

Want $E_S M_t = M_t$

(compute) $E_S M_t = E_S e^{\lambda W_t - \alpha t} = E_S e^{-\alpha t} e^{\lambda(W_t - W_S + W_S)} = e^{-\alpha t} E_S (e^{\lambda(W_t - W_S)} e^{\lambda W_S})$

$$= e^{-\alpha t} E_S (e^{\lambda(W_t - W_S)} e^{\lambda W_S})$$

At time $N \rightarrow$ Payoff $g(S_N) = f_N(S_N)$ ($f_N(x) = g(x)$)

Compute V_{N-1} : $V_{N-1} = \frac{1}{1+r} E_{N-1} V_N = \frac{1}{1+r} E_{N-1} f_N(S_N)$

$$= \frac{1}{1+r} E_{N-1} f_N(S_{N-1}, X_N)$$

$X_N = \begin{cases} u & \text{if } N^{\text{th}} \text{ coin} = H \\ d & \text{if } N^{\text{th}} \text{ coin} = T \end{cases}$

Indifference $\frac{1}{1+r} E_{N-1} [f_N(S_{N-1}, u) + f_N(S_{N-1}, d)] = \frac{1}{1+r} f_{N-1}(S_{N-1})$

$$f_{n-1}(x) = \frac{1}{1+n} \left[f_n(x) + f_n'(dx) \right]$$

Continue & write formula for $f_n(x)$ intervals of f_{n+1}

$$\int_0^T DdS_t$$

Riemann Stijjes

$$\lim_{|P| \rightarrow 0}$$

$$\sum_{i=1}^n (S_{t_{i+1}} - S_{t_i})$$

|||||

lim exists only if $V_{[0,T]} < \infty$

$$V_{[0,T]} = \sum |S_{t_{i+1}} - S_{t_i}|$$

$$E_s M_t = e^{-\alpha t} e^{\lambda W_s} E e^{\lambda(W_t - W_s)}$$

$$= e^{\lambda W_s - \alpha s} e^{-\alpha(t-s)} e^{\frac{\lambda^2}{2} (t-s)}$$