



$$\sum \tilde{f}_i = 1$$

$$\sum \tilde{f}_i f_i = 1 + r$$

$\left. \begin{array}{l} 2 \text{ Eq} \\ 3 \text{ unknowns} \end{array} \right\}$

Rule of thumb : ① # unknowns = # eq : unique sol

→ ② # unknowns > # eq : ∞ many sol

③ # unknowns < # eq : ~~unique sol~~
no solutions

$$X_0 = 0 = \underbrace{\Delta_0 S_0}_{\text{stock}} + \underbrace{\Gamma_0 V_0}_{\text{call opt}} - \underbrace{(\Delta_0 S_0 + \Gamma_0 V_0)}_{\text{cash.}}$$

Want $X_1 \geq 0$ on all evols

$$X_1 = \Delta_0 S_1 + \Gamma_0 (S_1 - \underline{1})^+ - (1+r)(\Delta_0 + \Gamma_0 V_0).$$