

Put/Call Parity

Call $(S_T - K)^+$

Put $(K - S_T)^+ = - (S_T - K)^-$

Buying a Call
Selling a Put

$$(S_T - K)^+ - (K - S_T)^+ = \begin{cases} S_T - K & S_T \geq K \\ -(K - S_T) & S_T < K \\ = S_T - K \end{cases}$$

$$S_T \geq K$$

$$S_T < K$$

→ T

Put = Payment - S_T + K

Time 0

$$C(T, X) \quad S_0 \quad \frac{K}{e^{r(T-t)}}$$

$$\underline{0 < k_1 < k_2}$$

European option pays

$$\rightarrow \underline{(S_T \wedge k_2) - k_1}^+ =$$

$$\begin{cases} 0 & S_T \leq k_1 \\ S_T - k_1 = (S_T - k_1)^+ & k_1 < S_T \leq k_2 \\ k_2 - k_1 = (k_2 - k_1)^+ & k_2 < S_T \end{cases}$$

$$S_T \leq k_1$$

$$k_1 < \underline{S_T} \leq k_2$$

$$k_2 < S_T$$

