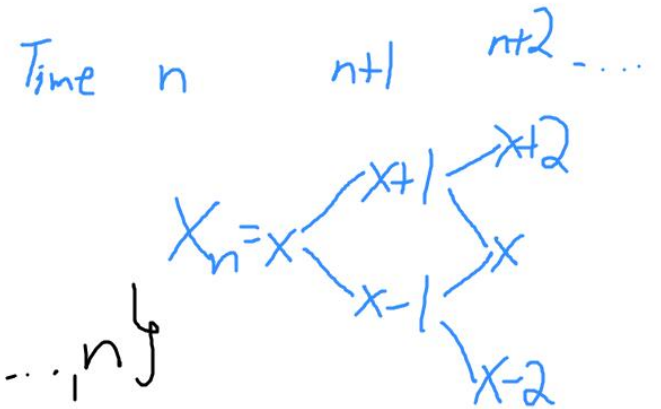


3 a)  $X_n = V_n^A - V_n^B$

IP of person (n+1) vote for A  $\frac{V_n^A}{n}$

$f_n(x) = \mathbb{P}(X_{n+1} > 0 \mid X_n = x)$   $x \in \{-n, -n+1, \dots, n\}$



$Y_n = \begin{cases} 1 & \text{if vote } n \text{ is for A} \\ 0 & \text{if vote } n \text{ is for B} \end{cases}$   $Y_n = \mathbb{1}_{\{\text{Vote } n \text{ is for A}\}}$

$V_{n+1}^A = V_n^A + Y_{n+1}$        $V_{n+1}^B = V_n^B + 1 - Y_{n+1}$

$X_{n+1} = X_n + 2Y_{n+1} - 1$

$\mathbb{P}(X_{n+1} = x \mid X_n = x)$

$\mathbb{P}(X_{n+r} = \bar{x} \mid X_n = x)$

$X_{n+1} \in \{X_n + 1, X_n - 1\}$

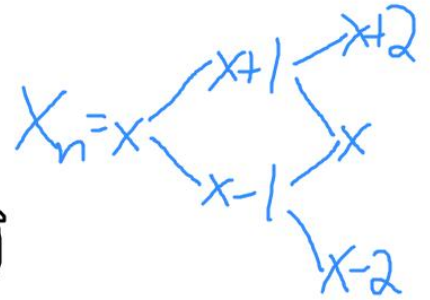
$$3a) X_n = V_n^A - V_n^B$$

IP of person (n+1) vote for A

$$\left( \frac{V_n^A}{n} \right)$$

$$f_n(x) = \mathbb{P}(X_{n+1} > 0 \mid X_n = x) \quad x \in \{-n, -n+1, \dots, n\}$$

Time n      n+1      n+2 ...



$$\mathbb{P}(X_{n+1} = x' \mid X_n = x) = \begin{cases} \frac{V_n^A}{n} & \text{if } x' = x+1 \\ 1 - \frac{V_n^A}{n} & \text{if } x' = x-1 \\ 0 & \text{otherwise} \end{cases}$$

$$\mathbb{P}(X_{n+2} = x+2 \mid X_n = x) = \mathbb{P}(X_{n+2} = X_{n+2})$$

$$\mathbb{P}(X_{n+2} = X_n) = \mathbb{P}(X_{n+2} = X_{n+1} + 1) \cdot \mathbb{P}(X_{n+1} = X_n - 1) \\ + \mathbb{P}(X_{n+2} = X_{n+1} - 1) \cdot \mathbb{P}(X_{n+1} = X_n + 1)$$

$$\mathbb{P}(X_{n+r} = \bar{x} \mid X_n = x)$$

2. American option intrinsic value  $(G_1, G_2, \dots, G_N) = G$   
 $V_n$  arbitrage-free price

a)  $V_\sigma = G_\sigma$  for some stopping time  
 $\sigma$  optimal time?

maximizes  $V_0^\sigma$   
 $\tau$  other stopping time

$$V_0^\sigma \geq V_0^\tau$$

$$V_0 = \max_{\tau \text{ stopping time}} V_0^\tau$$

$$V_0 = V_0^{\sigma^*}$$

$$\sigma^* = \min\{n \mid V_n = G_n\}$$