# Department of Mathematical Sciences Carnegie Mellon University

21-393 Operations Research II Test2

Name:\_\_\_\_\_

Problem	Points	Score
1	25	
2	30	
3	20	
4	25	
Total	100	

## Q1: (25pts) (a) Write down the dual of

maximise  $x_1 + 6x_2$ subject to  $2x_1 + 3x_2 \leq 12$  $6x_1 + x_2 \leq 8$  $x_1, x_2 \geq 0.$ 

(b) You are now given that the optimal solution to the above program is  $x_1 = 0, x_2 = 4$ . Use complementary slackness to solve the dual.

### Q2: (30pts)

Write down the Karush-Kuhn-Tucker conditions for the following problem:

minimise 
$$(x-1)^2 + (y-2)^2$$

subject to

 $2x + 3y_2 \ge 10$ 

Solve the problem by finding a solution to the KKT conditions.

#### Q3: (20pts)

Set up the initial tableau for solving the problem of Q2 by the *restricted* simplex algorithm. List the pairs of variables that cannot simultaneously be basic. —YOU DO NOT HAVE TO CONTINUE BEYOND THIS POINT IN THE SOLUTION OF THE PROBLEM

### Q4: (25pts)

Players A and B play the following game. A chooses a number  $x_A \in \{0, 1, 2, 3\}$  and B chooses a number  $x_B \in \{0, 1, 2\}$ . If  $x_A + x_B$  is odd, A wins a point, otherwise B wins a point.

Write down a linear program whose solution will produce an optimum strategy for A. YOU DO NOT HAVE TO SOLVE THE PROGRAM.