# Department of Mathematical Sciences Carnegie Mellon University <br> 21-393 Operations Research II <br> Test 1 

Name:

| Problem | Points | Score |
| :--- | :--- | :--- |
| 1 | 33 |  |
| 2 | 33 |  |
| 3 | 34 |  |
| Total | 100 |  |

Q1: (33pts)
Find a stable solution to the following game:

$$
\left[\begin{array}{cc}
3 & 4 \\
4 & -1
\end{array}\right]
$$

Q2: (33pts) Solve the following integer programming problem using branch and bound.

$$
\begin{aligned}
\begin{array}{l}
\operatorname{maximise} \\
\text { subject to }
\end{array} & 2 x_{1}+3 x_{2} \\
& x_{1}+2 x_{2} \leq 2 \\
& 3 x_{1}+x_{2} \leq 4 \\
x_{1}, x_{2} \geq 0 & \text { and integer. }
\end{aligned}
$$

Q3: (34pts) A student is preparing for four tests $T_{1}, T_{2}, T_{3}, T_{4}$ and only has 5 hours in which to study. The following table $S$ gives the number of points the student will get on $T_{i}$ if he/she spends $j$ hours studying for that test. Use Dynamic Programming to find the strategy that maximises the students points.

| Hours | $T_{1}$ | $T_{2}$ | $T_{3}$ | $T_{4}$ |
| :--- | :--- | :--- | :--- | :--- |
| 0 | 50 | 50 | 50 | 50 |
| 1 | 60 | 65 | 60 | 70 |
| 2 | 75 | 70 | 70 | 80 |
| 3 | 80 | 80 | 70 | 80 |
| 4 | 90 | 85 | 70 | 80 |
| 5 | 95 | 90 | 70 | 85 |

