

OPERATIONS RESEARCH II 21-393

Homework 3: Due Monday October 1.

Q1 Solve the following problem by a cutting plane algorithm:

$$\begin{array}{ll} \text{minimise} & 4x_1 + 5x_2 + 3x_3 \\ \text{subject to} & \\ & 2x_1 + x_2 - x_3 \geq 2 \\ & x_1 + 4x_2 + x_3 \geq 13 \end{array}$$

$$x_1, x_2, x_3 \geq 0 \text{ and integer.}$$

- Q2** Formulate the following as an integer program: There are n students and exams $E_1, E_2, \dots, E_m \subseteq [n]$ need to be scheduled. There are s rooms available and each room can hold r students. The rules are
- (i) A student must not be asked to take more than one exam per day;
 - (ii) Several different exams can be held in the same room provided there is capacity in the room to hold the students.
 - (iii) No student has to take 3 exams in 3 consecutive days.

The problem is to minimise the number of days needed to carry out all of the exams.

- Q3** An assembly line consists of a sequence of locations called work stations. The manufacture of a certain object requires m separate jobs to be undertaken with job i requiring t_i minutes. The jobs are to be allocated to work stations so that each station completes a set of jobs and then passes the object onto the next station on the line and waits to receive the next object from the previous station on the line. The combined time of all jobs assigned to any station must not exceed T the cycle time. Also there are a number of precedence relations between jobs indicated by the digraph $D = (V, A)$ where $(i, j) \in A$ if job i must precede job j . The problem is to open as few work stations as possible consistent with the cycle time. Formulate this as an integer programming problem.