

OPERATIONS RESEARCH II 21-393

Homework 4: Due Wednesday October 24.

1. Formulate the following as an integer program: An assembly line consists of a sequence of locations called work stations. The manufacture of a certain object requires m separate jobs to be undertaken with job i requiring t_i minutes. The jobs are to be allocated to work stations so that each station completes a set of jobs and then passes the object onto the next station on the line and waits to receive the next object from the previous station on the line. The combined time of all jobs assigned to any station must not exceed T the cycle time. Also there are a number of precedence relations between jobs indicated by the digraph $D = (V, A)$ where $(i, j) \in A$ if job i must precede job j . The problem is to open as few work stations as possible consistent with the cycle time.
2. Solve the following problem by a cutting plane algorithm:

$$\begin{array}{llllll} \text{minimise} & 4x_1 & + & 5x_2 & + & 3x_3 \\ \text{subject to} & & & & & \\ & 2x_1 & + & x_2 & - & x_3 & \geq & 2 \\ & x_1 & + & 4x_2 & + & x_3 & \geq & 13 \\ & x_1, x_2, x_3 \geq 0 & \text{and integer.} \end{array}$$

3. Solve the following problem by a branch and bound algorithm:

$$\begin{array}{llllll} \text{Maximise} & 4x_1 & - & 2x_2 & + & 7x_3 & - & x_4 \\ \text{subject to} & & & & & & & \\ & x_1 & & & + & 5x_3 & & \leq 10 \\ & x_1 & + & x_2 & - & x_3 & & \leq 1 \\ & 6x_1 & - & 5x_2 & & & & \leq 0 \\ & -x_1 & & & + & 2x_3 & - & 2x_4 \leq 3 \\ & x_1, x_2, x_3, x_4 \geq 0. \\ & x_1, x_2, x_3 \text{ integer.} \end{array}$$