## 21-301 Combinatorics Homework 5

Due: Monday, October 27

- 1. Let  $x_1, x_2, \ldots, x_n$  be real numbers such that  $x_i \geq 1$  for  $i = 1, 2, \ldots, n$ . Let J be any open interval of width 2. Show that of the  $2^n$  sums  $\sum_{i=1}^n \varepsilon_i x_i$ ,  $(\varepsilon_i = \pm 1)$ , at most  $\binom{n}{\lfloor n/2 \rfloor}$  lie in J.
- 2. Suppose that we two-color the edges of  $K_6$  Red and Blue. Show that there are at least two monochromatic triangles.
- 3. Show that  $r(C_4, C_4) = 6$ , where  $C_4$  denotes a cycle of length 4.