## 21-301 Combinatorics Homework 1

Due: Monday, September 8

- 1. How many sequences  $(a_1, a_2, \dots, a_m) \in [n]^m$  satisfy  $a_1 < a_2 < \dots < a_m$ ? How many satisfy  $a_1 \le a_2 \le \dots \le a_m$ ?
- 2. Suppose that a round table has 3n labelled seats. Suppose that n families arrive consisting of man/woman/child. They are to be seated round the table in triples: adult, child, adult. How many ways of seating the guests are there so that no family sits together as a complete triple of adult, child, adult.
- 3. Suppose that we have 2n distinguishable balls. Suppose that there are n colors and that we have 2 balls of each color. How many ways are there of placing the balls into n distinguishable boxes, two balls per box, so that there are exactly k boxes containing balls of the same color?