

11\26\2007

⋮ missing due to computer
⋮ problems.
⋮

r	b
r	r

$\equiv rbr r$

~~$g(x)$~~

$g * x$

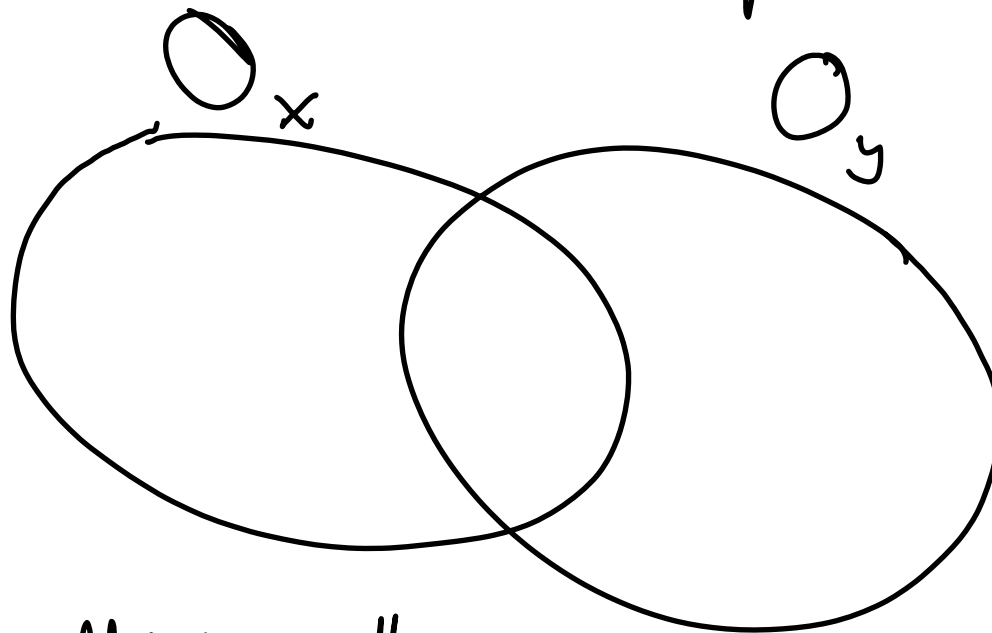
Orbit O_x of $x \in X$.

$$O_x = \{ y : y = g * x \text{ for some } g \in G \}$$

$\Rightarrow O_y = O_x$

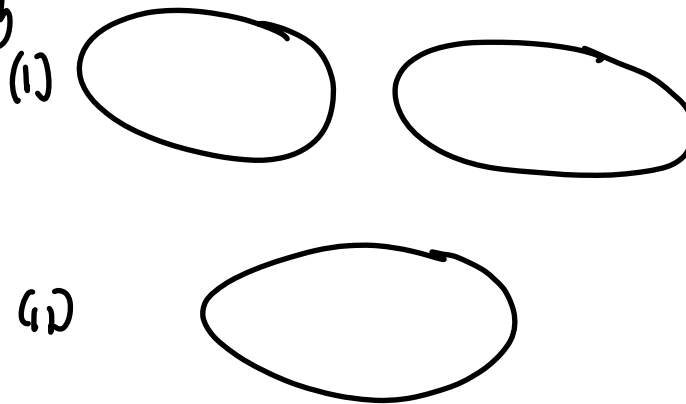
Question: How many orbits are there

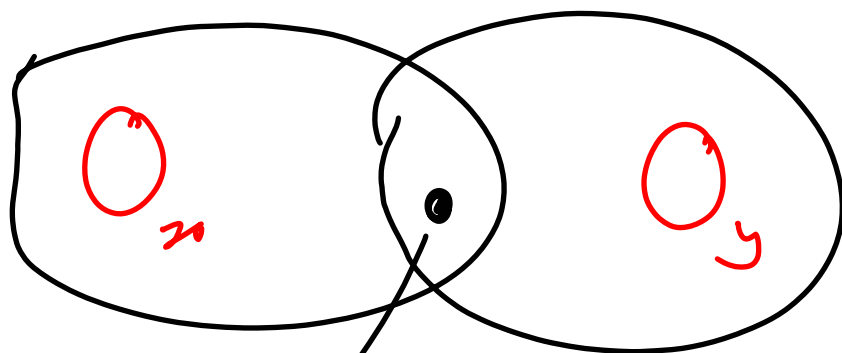
Claim: The orbits partition X .



To show this is really

if 2 orbits intersect in a non-empty set then they are equal.





$$g_1 * x = g_2 * y \quad g_1, g_2 \in G$$

$$g_1^{-1} * (g_1 * x) = g_1^{-1} * (g_2 * y)$$

$$(g_1^{-1} \circ g_1) * x = (g_1^{-1} \circ g_2) * y$$

$$x = h * y \quad h = g_1^{-1} \circ g_2 \in G.$$

$$\begin{aligned} z \in O_x: z = g * x &= (g \circ h) * y \\ \Rightarrow z \in O_y. \quad O_x \subseteq O_y \subseteq O_x. \end{aligned}$$

$H \subseteq G$ is a subgroup if

(i) $e \in H$

(ii) $g_1, g_2 \in H \Rightarrow g_1 g_2 \in H$

(iii) $g \in H \Rightarrow g^{-1} \in H.$

Stabiliser $S_x = \{g : g * x = x\}$

Amk prove $\# \text{ orbits} = \frac{1}{|G|} \sum_{x \in X} |S_x|.$