

Large Graph Mining: Power Tools and a Practitioner's guide

Task 3: Recommendations & proximity

Faloutsos, Miller & Tsourakakis

CMU



Outline

- Introduction – Motivation
- Task 1: Node importance
- Task 2: Community detection
- ➔ • **Task 3: Recommendations**
- Task 4: Connection sub-graphs
- Task 5: Mining graphs over time
- Task 6: Virus/influence propagation
- Task 7: Spectral graph theory
- Task 8: Tera/peta graph mining: hadoop
- Observations – patterns of real graphs
- Conclusions



Acknowledgement:

Most of the foils in ‘Task 3’ are by



Hanghang TONG

www.cs.cmu.edu/~htong

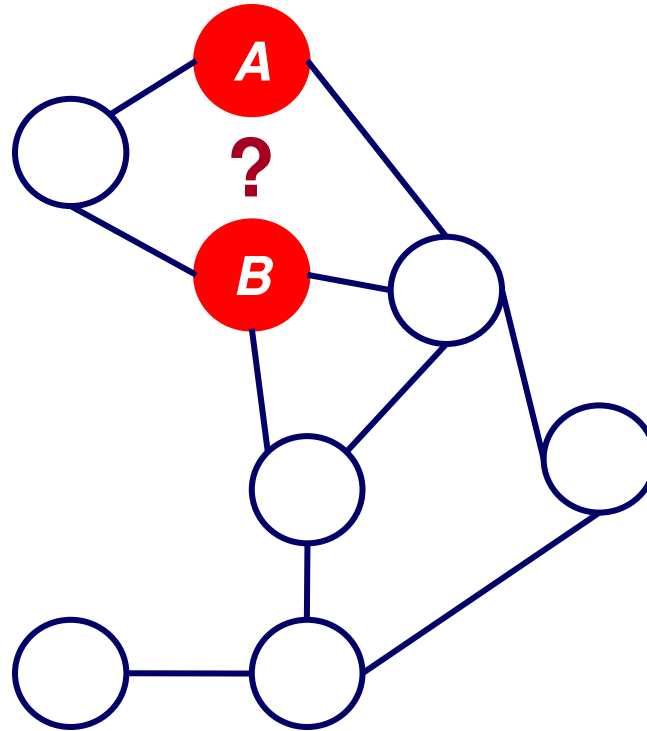


Detailed outline

- ➔ • Problem defn and motivation
- Solution: Random walk with restarts
- Efficient computation
- Case study: image auto-captioning
- Extensions: bi-partite graphs; tracking
- Conclusions



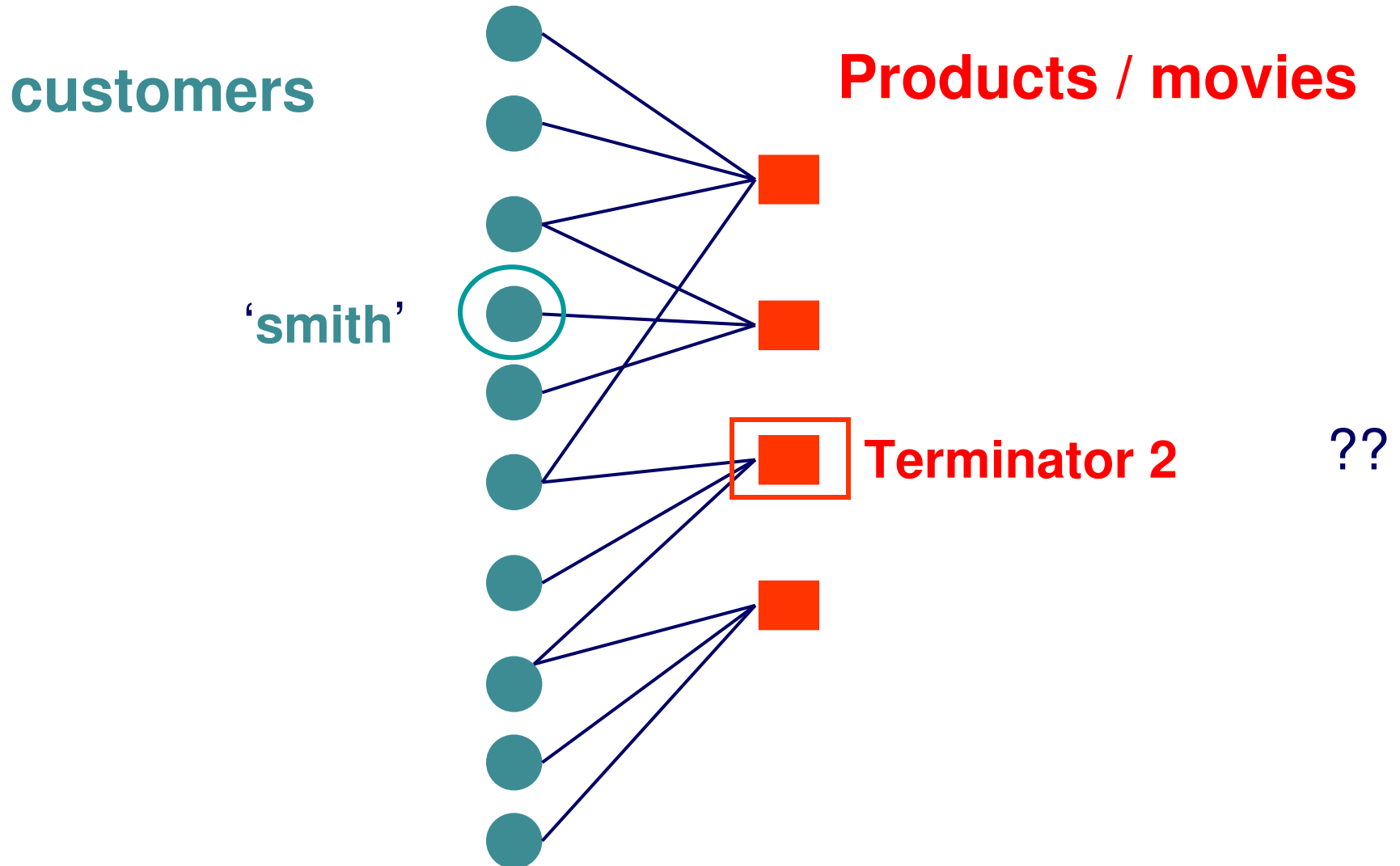
Motivation: Link Prediction



Should we introduce
Mr. A to Mr. B?



Motivation - recommendations





Answer: proximity

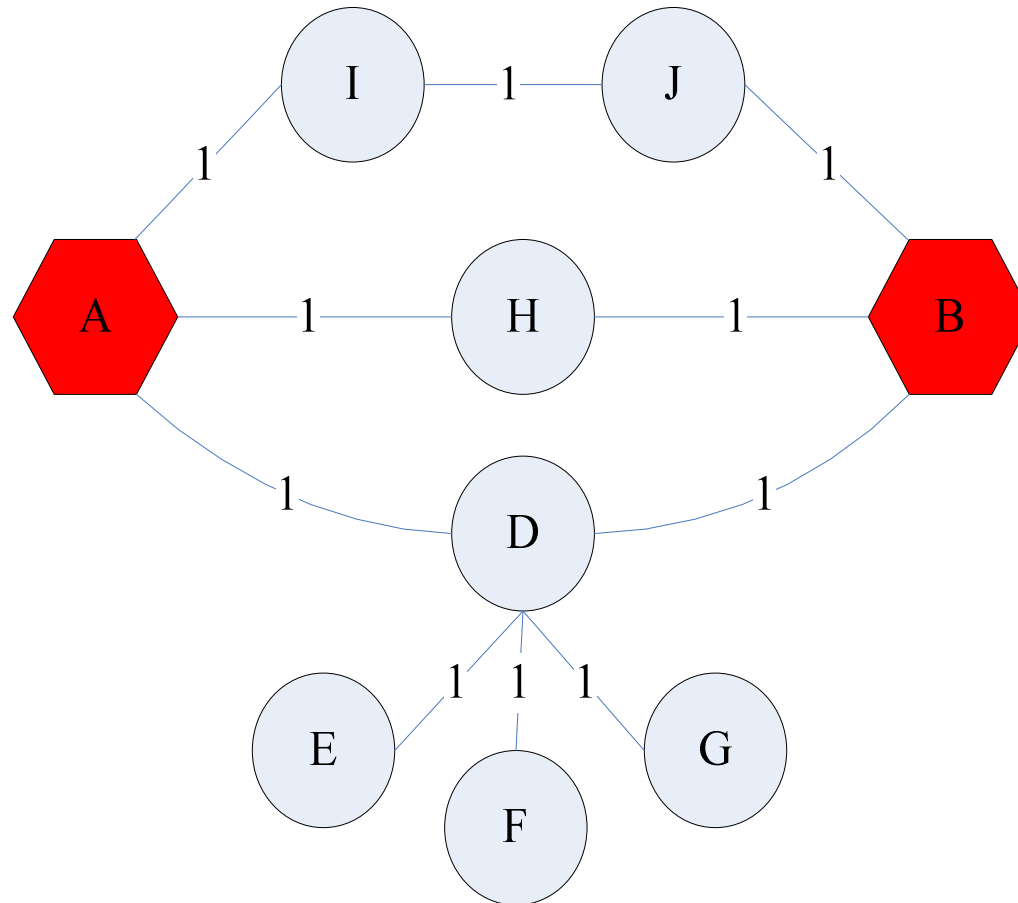
- ‘yes’, if ‘A’ and ‘B’ are ‘close’
- ‘yes’, if ‘smith’ and ‘terminator 2’ are ‘close’

QUESTIONS in this part:

- How to measure ‘closeness’/proximity?
- How to do it quickly?
- What else can we do, given proximity scores?



How close is 'A' to 'B'?



a.k.a Relevance, Closeness, 'Similarity'...



Why is it useful?

- Recommendation

And many more

- **Image captioning** [Pan+]
- **Conn. / CenterPiece subgraphs** [Faloutsos+], [Tong+], [Koren+]

and

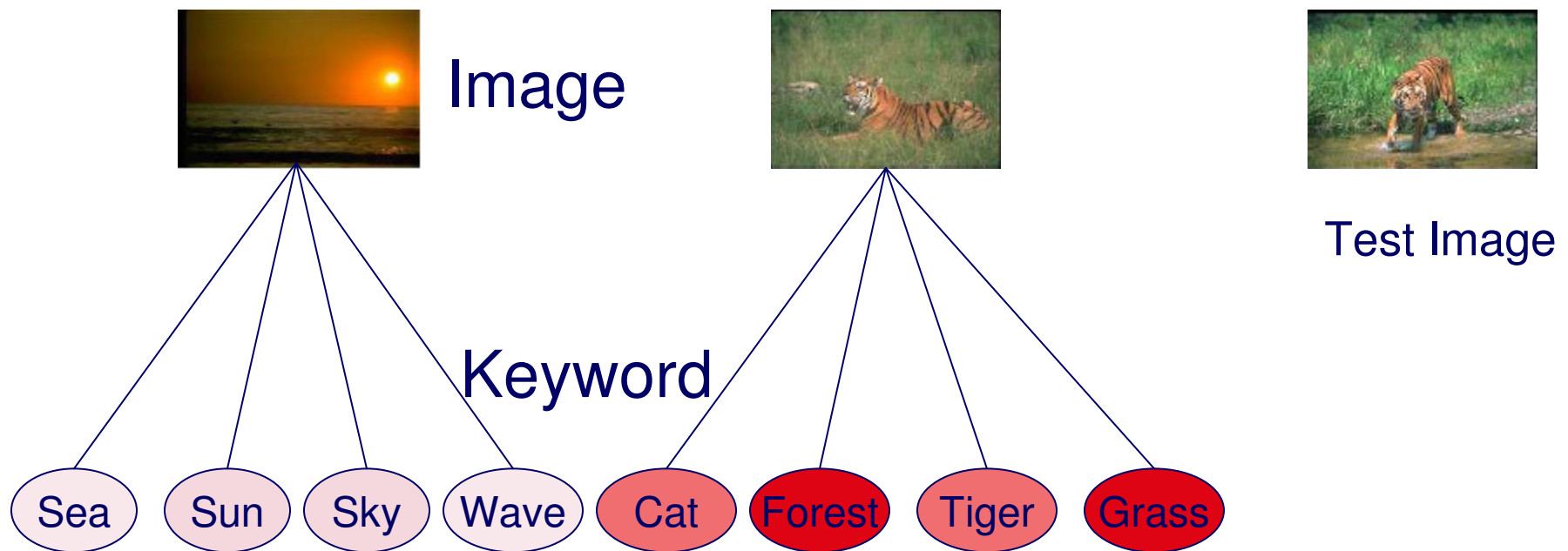
- Link prediction [Liben-Nowell+], [Tong+]
- Ranking [Haveliwala], [Chakrabarti+]
- Email Management [Minkov+]
- Neighborhood Formulation [Sun+]
- Pattern matching [Tong+]
- Collaborative Filtering [Fouss+]
- ...



CMU SCS

Region

Automatic Image Captioning



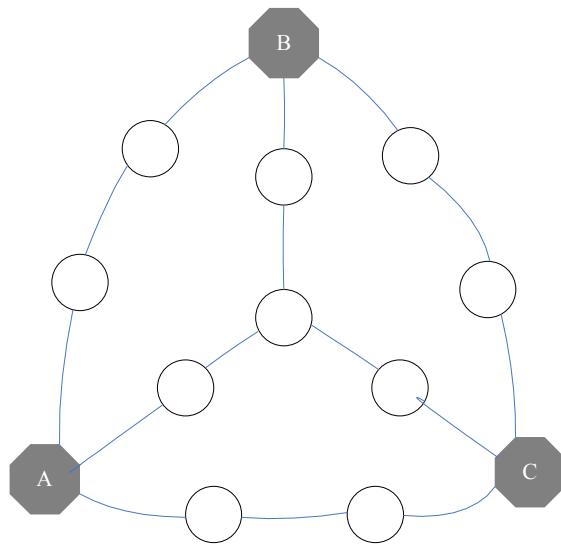
Q: How to assign keywords to the test image?

A: **Proximity!** [Pan+ 2004]

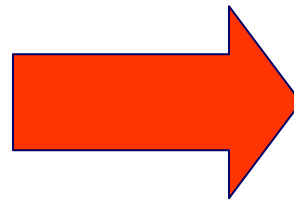


Center-Piece Subgraph(CePS)

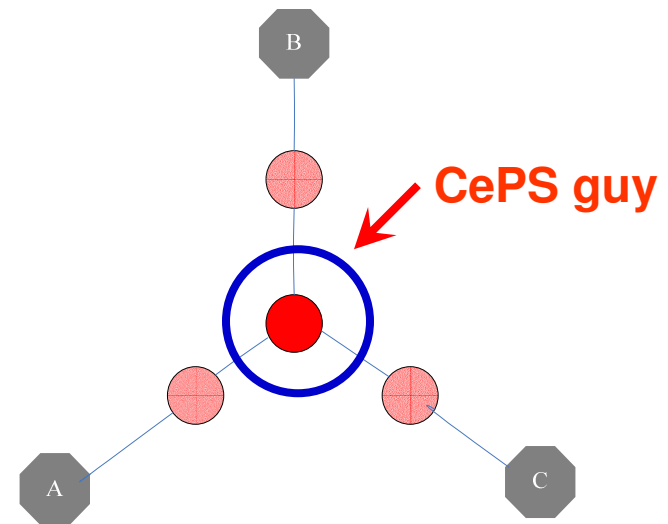
Input



Original Graph



Output



CePS

Q: How to find hub for the black nodes?

A: Proximity! [Tong+ KDD 2006]



Detailed outline

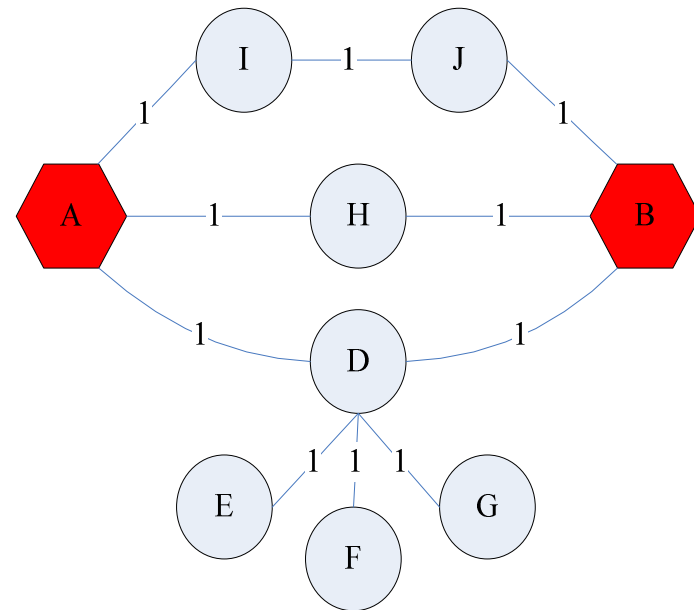
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How close is 'A' to 'B'?

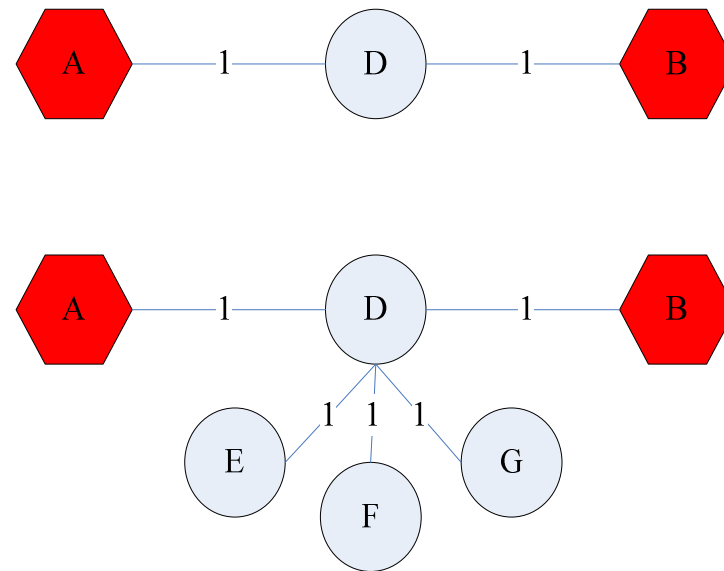
Should be close, if they have

- many,
- short
- 'heavy' paths





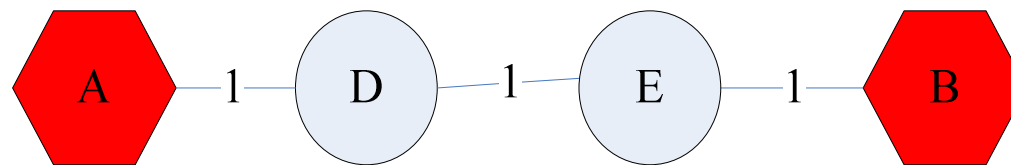
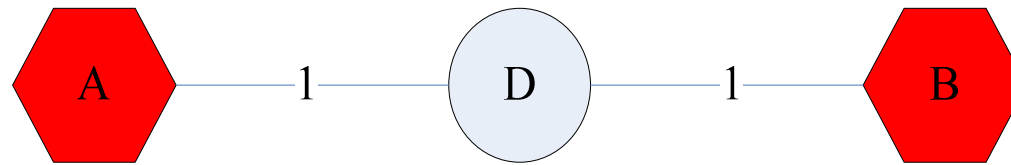
Why not shortest path?



A: 'pizza delivery guy' problem



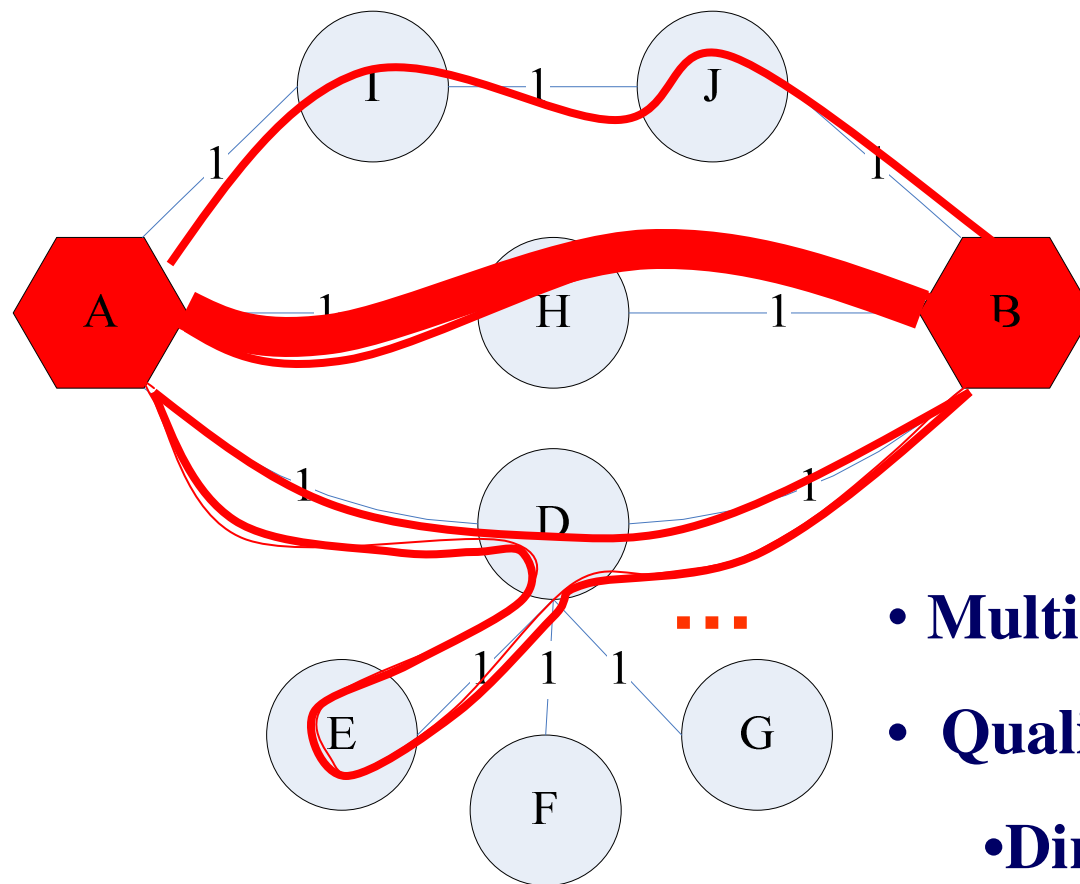
Why not max. netflow?



A: No penalty for long paths



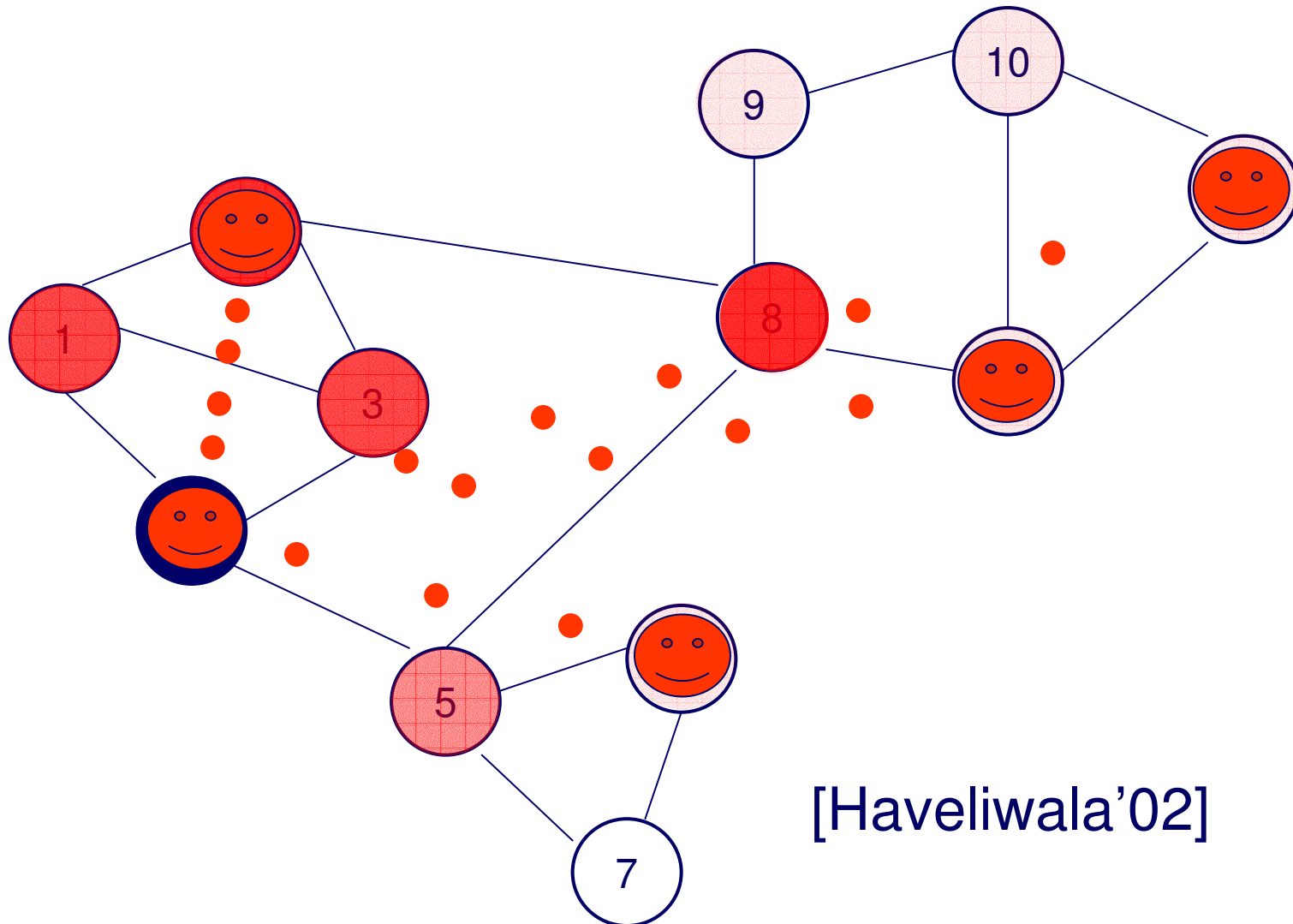
What is a ``good'' Proximity?



- Multiple Connections
- Quality of connection
 - Direct & In-directed Conns
 - Length, Degree, Weight...



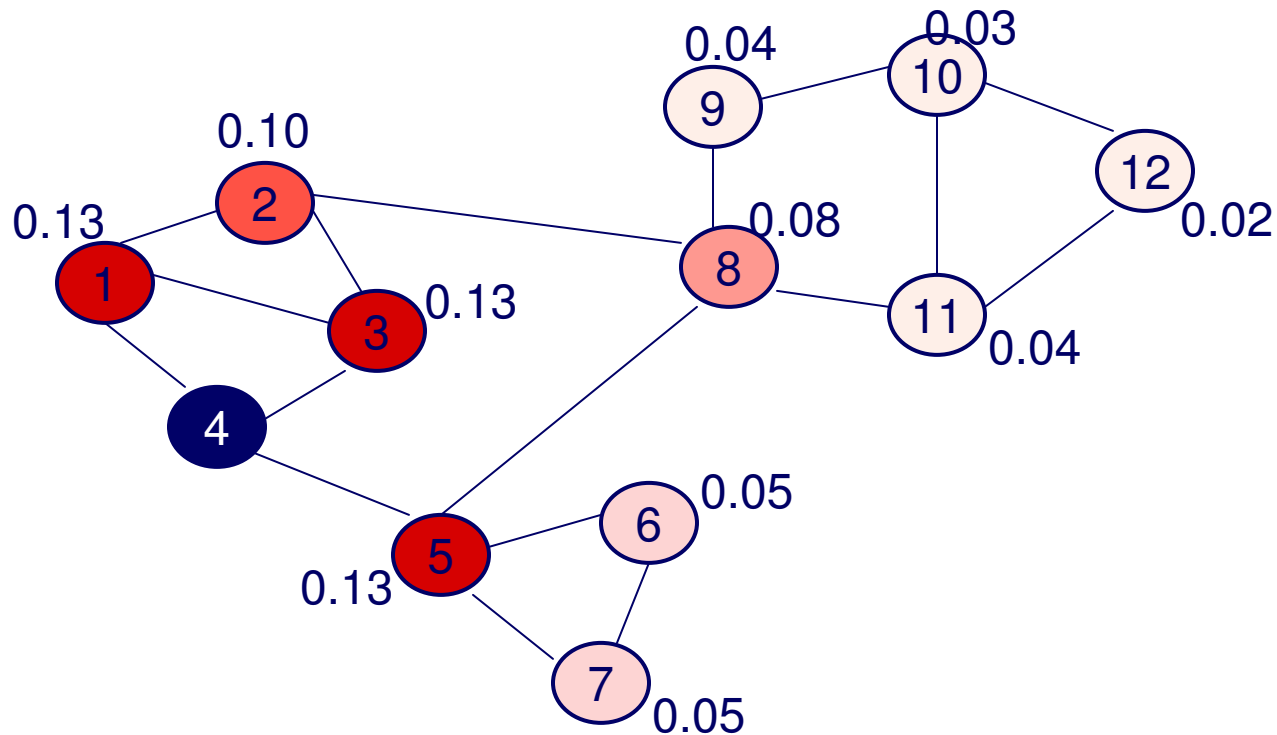
Random walk with restart



[Haveliwala'02]



Random walk with restart



Nearby nodes, higher scores

More red, more relevant

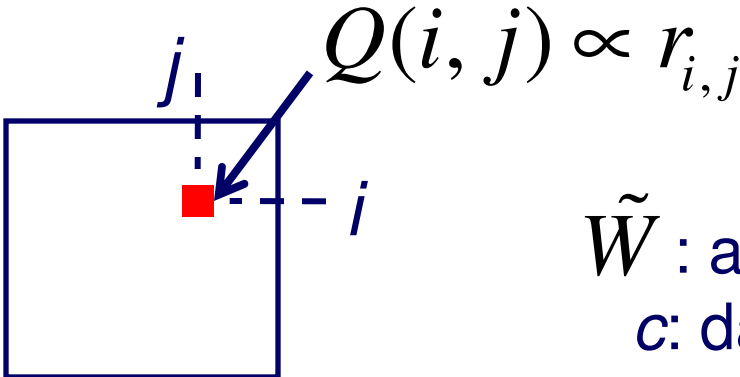
	Node 4
Node 1	0.13
Node 2	0.10
Node 3	0.13
Node 4	0.22
Node 5	0.13
Node 6	0.05
Node 7	0.05
Node 8	0.08
Node 9	0.04
Node 10	0.03
Node 11	0.04
Node 12	0.02

Ranking vector

\vec{r}_4



Why RWR is a good score?

$$Q = (I - c\tilde{W})^{-1} =$$


$Q(i, j) \propto r_{i, j}$

\tilde{W} : adjacency matrix.
 c : damping factor

$$Q = c \boxed{\tilde{W}} + c^2 \boxed{\tilde{W}^2} + c^3 \boxed{\tilde{W}^3} + \dots$$

all paths from i to j with length **1**

all paths from i to j with length **2**

all paths from i to j with length **3**



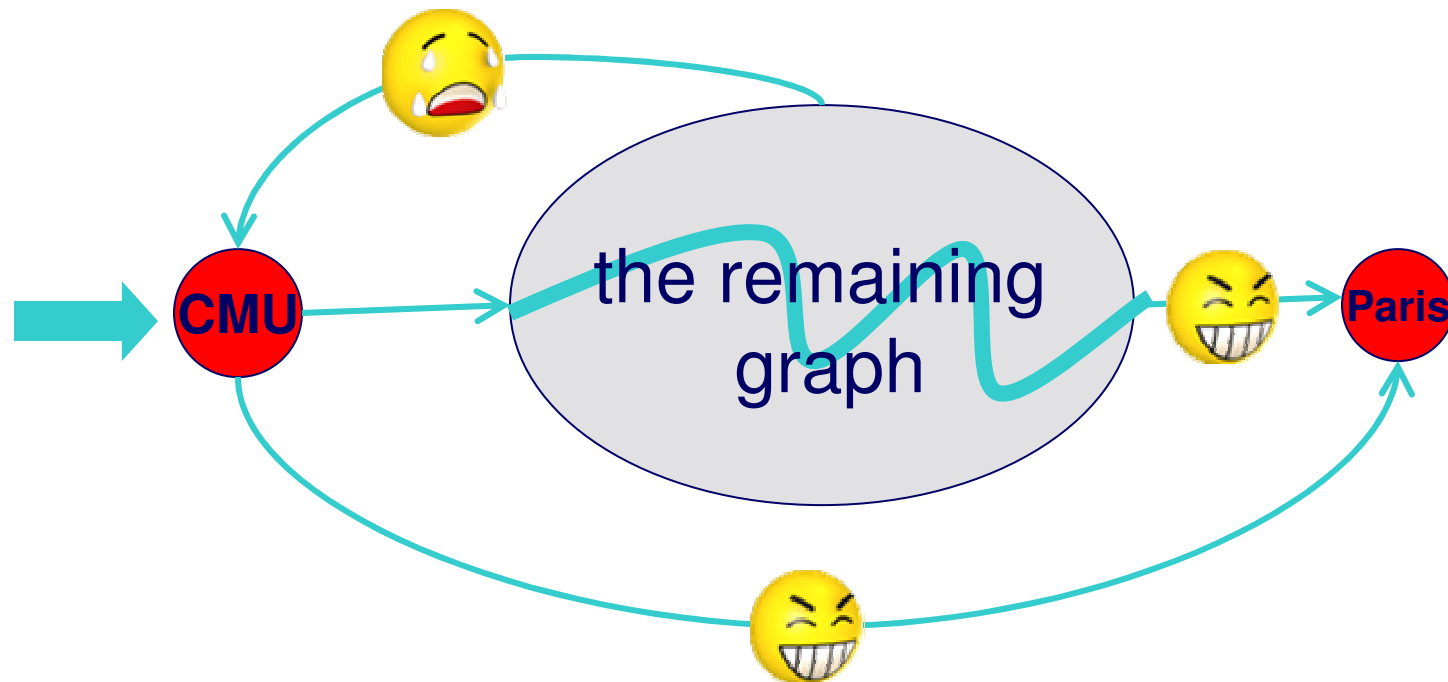
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 - ➔ – variants
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Variant: escape probability

- Define Random Walk (RW) on the graph
- $\text{Esc_Prob}(\text{CMU} \rightarrow \text{Paris})$
 - Prob (starting at CMU, reaches Paris before returning to CMU)





Other Variants

- Other measure by RWs
 - Community Time/Hitting Time [Fouss+]
 - SimRank [Jeh+]
- Equivalence of Random Walks
 - Electric Networks:
 - EC [Doyle+]; SAEC[Faloutsos+]; CFEC[Koren+]
 - Spring Systems
- Katz [Katz], [Huang+], [Scholkopf+]
- Matrix-Forest-based Alg [Chobotarev+]



Other Variants

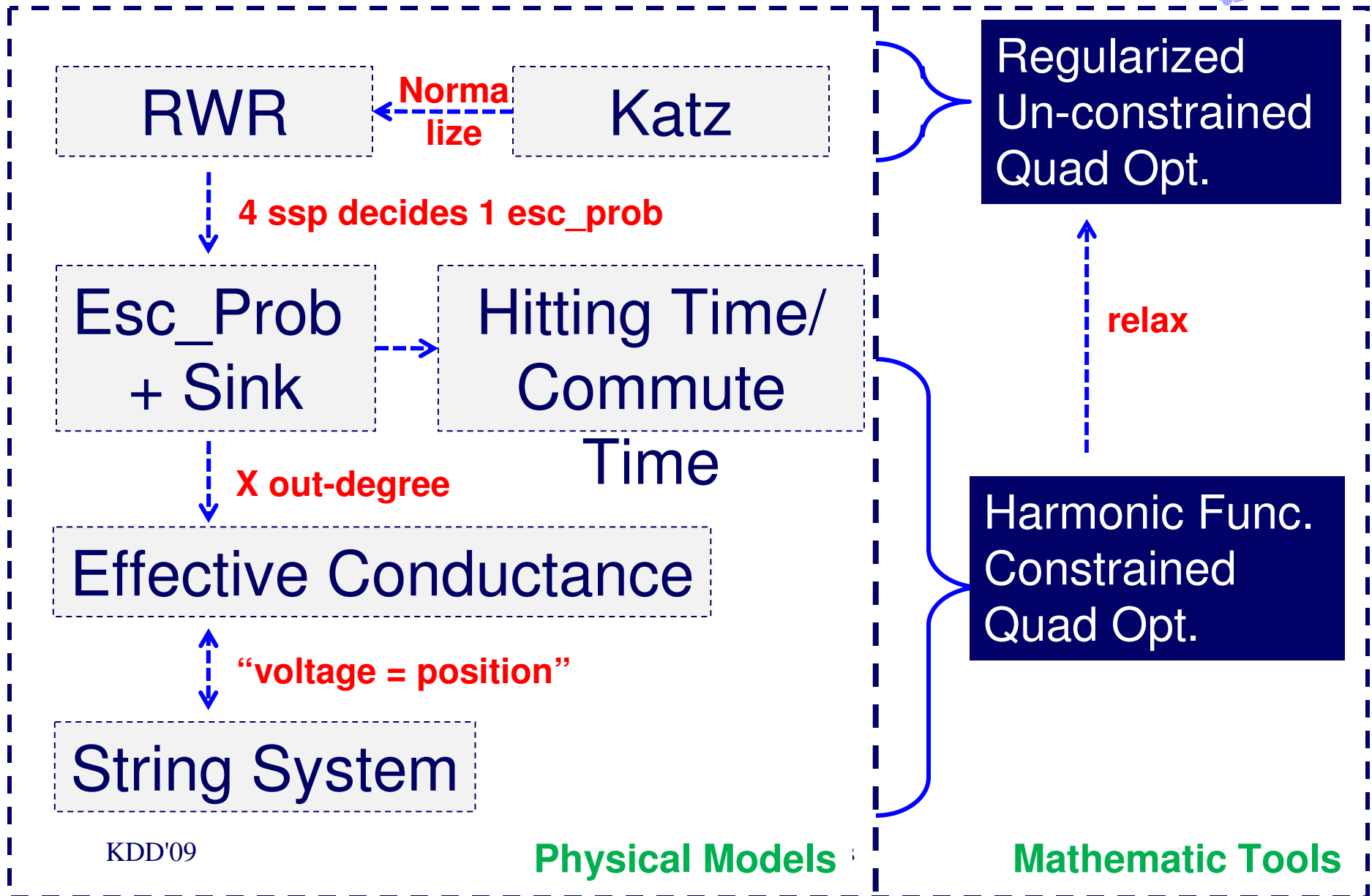
- Other measure by RWs
 - Community Time/Hitting Time [Fouss+]
 - SimRank [Jeh+]

All are “related to” or “similar to”
random walk with restart!

- Spring Systems
- Katz [Katz], [Huang+], [Scholkopf+]
- Matrix-Forest-based Alg [Chobotarev+]

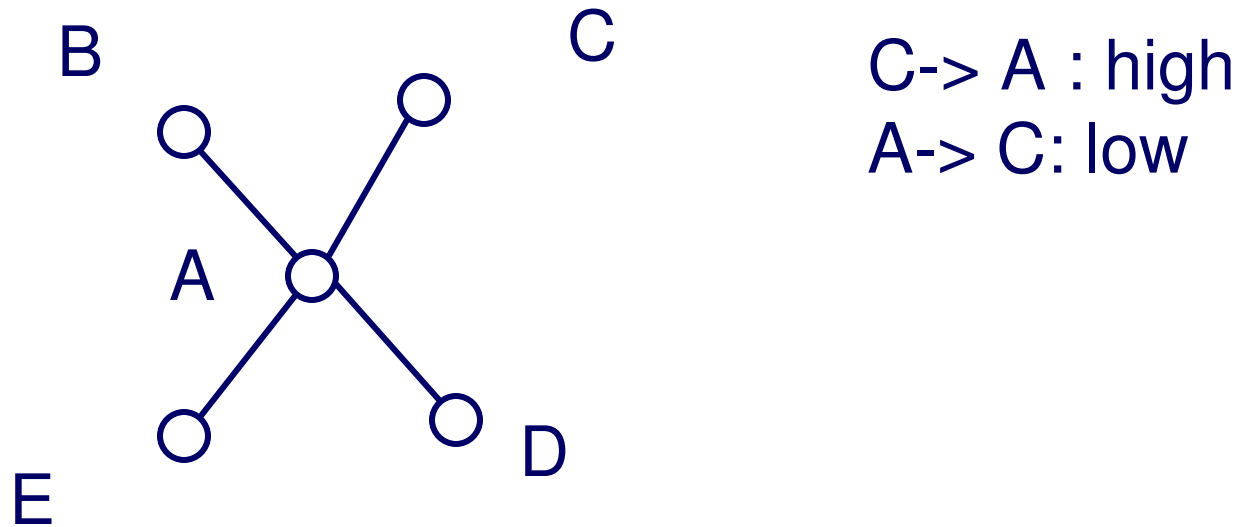


Map of proximity measurements

details



Notice: Asymmetry (even in undirected graphs)





Summary of Proximity Definitions

- Goal: Summarize multiple relationships
- Solutions
 - **Basic**: Random Walk with Restarts
 - [Haweliwala'02] [Pan+ 2004][Sun+ 2006][Tong+ 2006]
 - **Properties**: Asymmetry
 - [Koren+ 2006][Tong+ 2007] [Tong+ 2008]
 - **Variants**: Esc_Prob and many others.
 - [Faloutsos+ 2004] [Koren+ 2006][Tong+ 2007]



Detailed outline

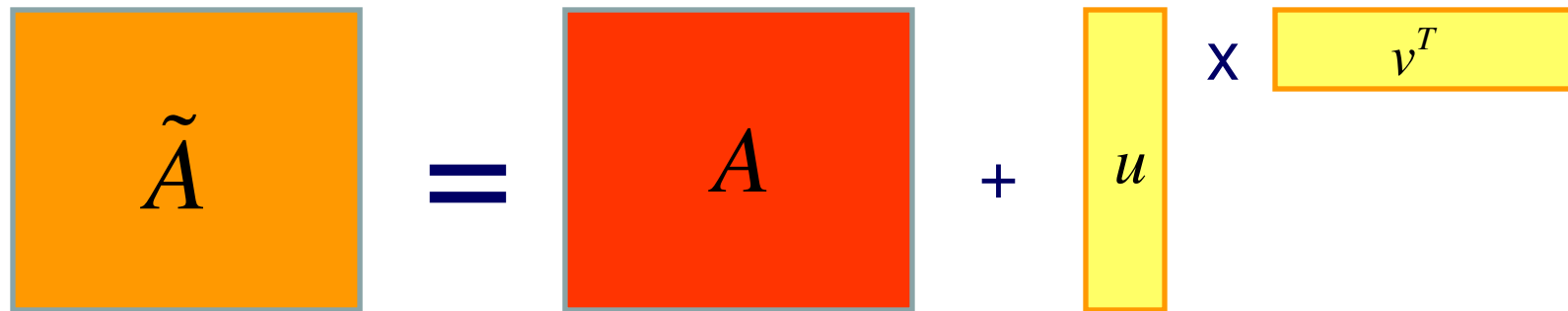
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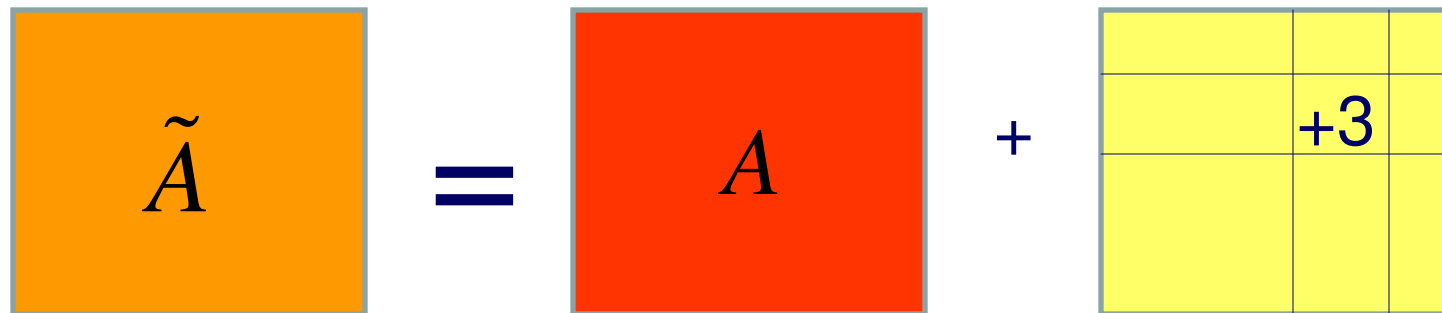


Preliminary: Sherman–Morrison Lemma

details

If:

$$\tilde{A} = A + u v^T$$


$$\tilde{A} = A + \begin{bmatrix} & & \\ & +3 & \\ & & \end{bmatrix}$$




Preliminary: Sherman–Morrison Lemma

details

If:

$$\tilde{A} = A + u \cdot v^T$$

Then:

$$\tilde{A}^{-1} = (A + u \cdot v^T)^{-1} = A^{-1} - \frac{A^{-1} \cdot u \cdot v^T A^{-1}}{1 + v^T \cdot A^{-1} \cdot u}$$



Sherman – Morrison Lemma – intuition:

- Given a small perturbation on a matrix
 $A \rightarrow A'$
- We can quickly update its inverse



SM: The block-form

details

A	B
C	D

$$\begin{bmatrix} A & B \\ C & D \end{bmatrix}^{-1} = \begin{bmatrix} A^{-1} + A^{-1}B(D - CA^{-1}B)^{-1}CA^{-1} & -A^{-1}B(D - CA^{-1}B)^{-1} \\ -(D - CA^{-1}B)^{-1}CA^{-1} & (D - CA^{-1}B)^{-1} \end{bmatrix}$$

Or...

$$\begin{bmatrix} A & B \\ C & D \end{bmatrix}^{-1} = \begin{bmatrix} (A - BD^{-1}C)^{-1} & -A^{-1}B(D - CA^{-1}B)^{-1} \\ -D^{-1}C(A - BD^{-1}C)^{-1} & (D - CA^{-1}B)^{-1} \end{bmatrix}$$

And many other variants...

Also known as Woodbury Identity



SM Lemma: Applications

- RLS (Recursive least squares)
 - and almost any algorithm in time series!
- Kalman filtering
- Incremental matrix decomposition
- ...
- ... and all the fast solutions we will introduce!

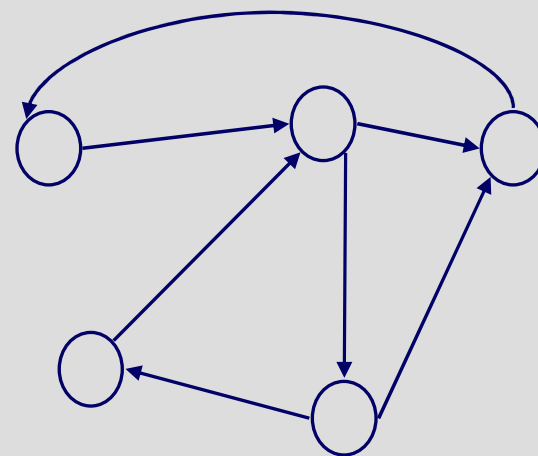
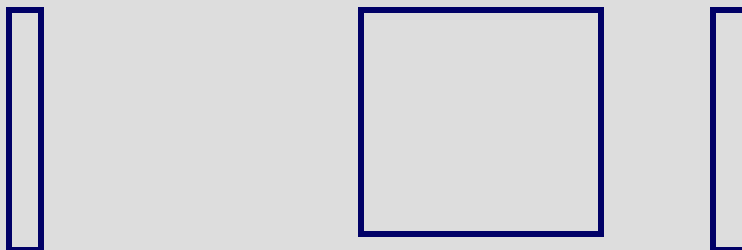


Reminder: PageRank

- With probability $1-c$, fly-out to a random node
- Then, we have

$$\mathbf{p} = c \mathbf{B} \mathbf{p} + (1-c)/n \mathbf{1} \Rightarrow$$

$$\mathbf{p} = (1-c)/n [\mathbf{I} - c \mathbf{B}]^{-1} \mathbf{1}$$





$$\mathbf{p} = c \mathbf{B} \mathbf{p} + (1-c)/n \mathbf{1}$$

$$\vec{r}_i = c \tilde{W} \vec{r}_i + (1-c) \vec{e}_i$$

**The only
difference**

Ranking vector

Adjacency matrix

Restart p

Starting vector



Computing RWR

$$\mathbf{p} = c \mathbf{B} \mathbf{p} + (1-c)/n \mathbf{1}$$

$$\vec{r}_i = c \tilde{W} \vec{r}_i + (1-c) \vec{e}_i$$

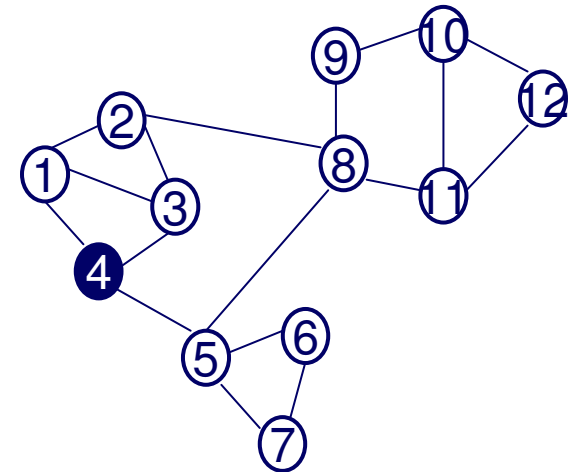
Ranking vector

Adjacency matrix

Restart p

Starting vector





$$\begin{array}{c}
 \begin{pmatrix} 0.13 \\ 0.10 \\ 0.13 \\ 0.22 \\ 0.13 \\ 0.05 \\ 0.05 \\ 0.08 \\ 0.04 \\ 0.03 \\ 0.04 \\ 0.02 \end{pmatrix} \\
 n \times 1
 \end{array}
 = 0.9 \times
 \begin{array}{c}
 \begin{pmatrix} 0 & 1/3 & 1/3 & 1/3 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 1/3 & 0 & 1/3 & 0 & 0 & 0 & 0 & 1/4 & 0 & 0 & 0 & 0 \\ 1/3 & 1/3 & 0 & 1/3 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 1/3 & 0 & 1/3 & 0 & 1/4 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 1/3 & 0 & 1/2 & 1/2 & 1/4 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 1/4 & 0 & 1/2 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 1/4 & 1/2 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 1/3 & 0 & 0 & 1/4 & 0 & 0 & 0 & 1/2 & 0 & 1/3 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 1/4 & 0 & 1/3 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 1/2 & 0 & 1/3 & 1/2 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 1/4 & 0 & 1/3 & 0 & 1/2 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 1/3 & 1/3 & 0 & 0 \end{pmatrix} \\
 n \times n
 \end{array}
 + 0.1 \times
 \begin{array}{c}
 \begin{pmatrix} 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \end{pmatrix} \\
 n \times 1
 \end{array}$$






Q: Given query i , how to solve it?

$$\begin{array}{c} \left\{ \begin{array}{c} ? \\ \end{array} \right\} = 0.9 \times \begin{pmatrix} 0 & 1/3 & 1/3 & 1/3 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 1/3 & 0 & 1/3 & 0 & 0 & 0 & 0 & 1/4 & 0 & 0 & 0 & 0 \\ 1/3 & 1/3 & 0 & 1/3 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 1/3 & 0 & 1/3 & 0 & 1/4 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 1/3 & 0 & 1/2 & 1/2 & 1/4 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 1/4 & 0 & 1/2 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 1/4 & 1/2 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 1/3 & 0 & 0 & 1/4 & 0 & 0 & 0 & 1/2 & 0 & 1/3 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 1/4 & 0 & 1/3 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 1/2 & 0 & 1/3 & 1/2 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 1/4 & 0 & 1/3 & 0 & 1/2 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 1/3 & 1/3 & 0 \end{pmatrix} \left\{ \begin{array}{c} ? \\ \end{array} \right\} + 0.1 \times \begin{pmatrix} 0 \\ 0 \\ 0 \\ 0 \\ 1 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \end{pmatrix}$$

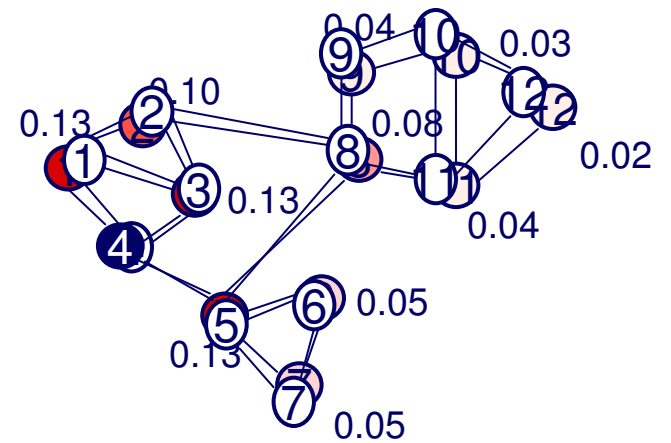
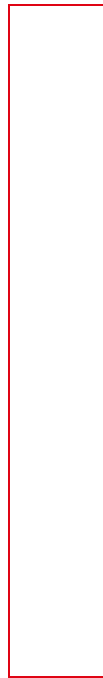
 **Ranking vector**  **Adjacency matrix**  **Ranking vector**  **Starting vector**

 **Query**



PreCompute

R:



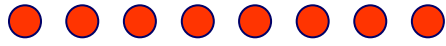
$$R = C \times Q$$

$$Q = (I - c\tilde{W})^{-1}$$

KDD 09

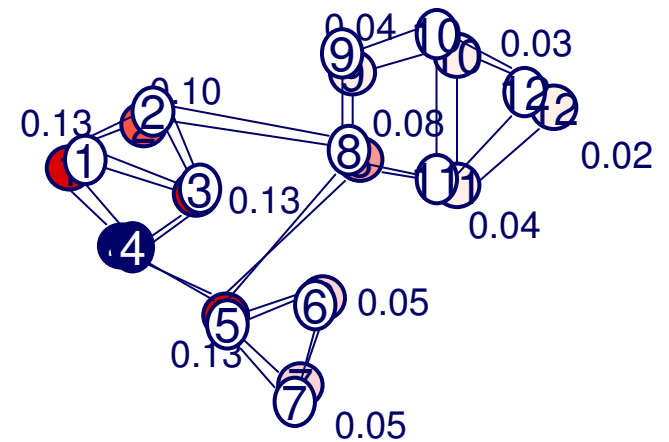


PreCompute: $Q = (I - c\tilde{W})^{-1}$



$$Q = (I - c\tilde{W})^{-1}$$

0.13	1.29
0.10	0.96
0.13	1.29
0.22	2.06
0.13	1.27
0.05 ← 0.1x	0.52
0.05	0.52
0.08	0.82
0.04	0.28
0.03	0.34
0.04	0.38
0.02	0.21



Fast on-line response



Heavy pre-computation/storage cost

KD.

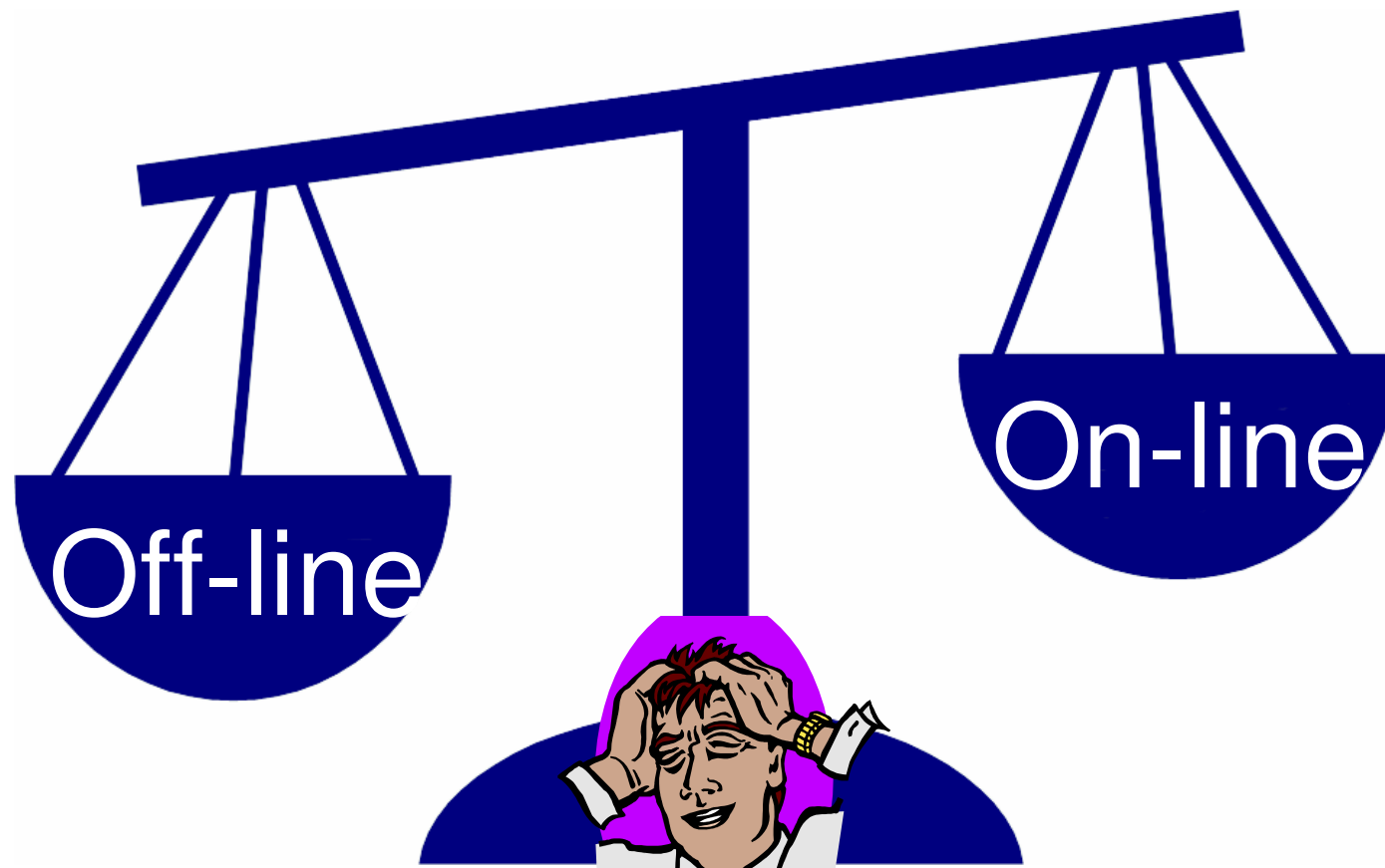
$O(n^3)$ iller, Tsourakakis

$O(n^2)$

P3-39



Q: How to Balance?





How to balance?

Idea ('B-Lin')

- Break into communities
- Pre-compute all, within a community
- Adjust (with S.M.) for 'bridge edges'

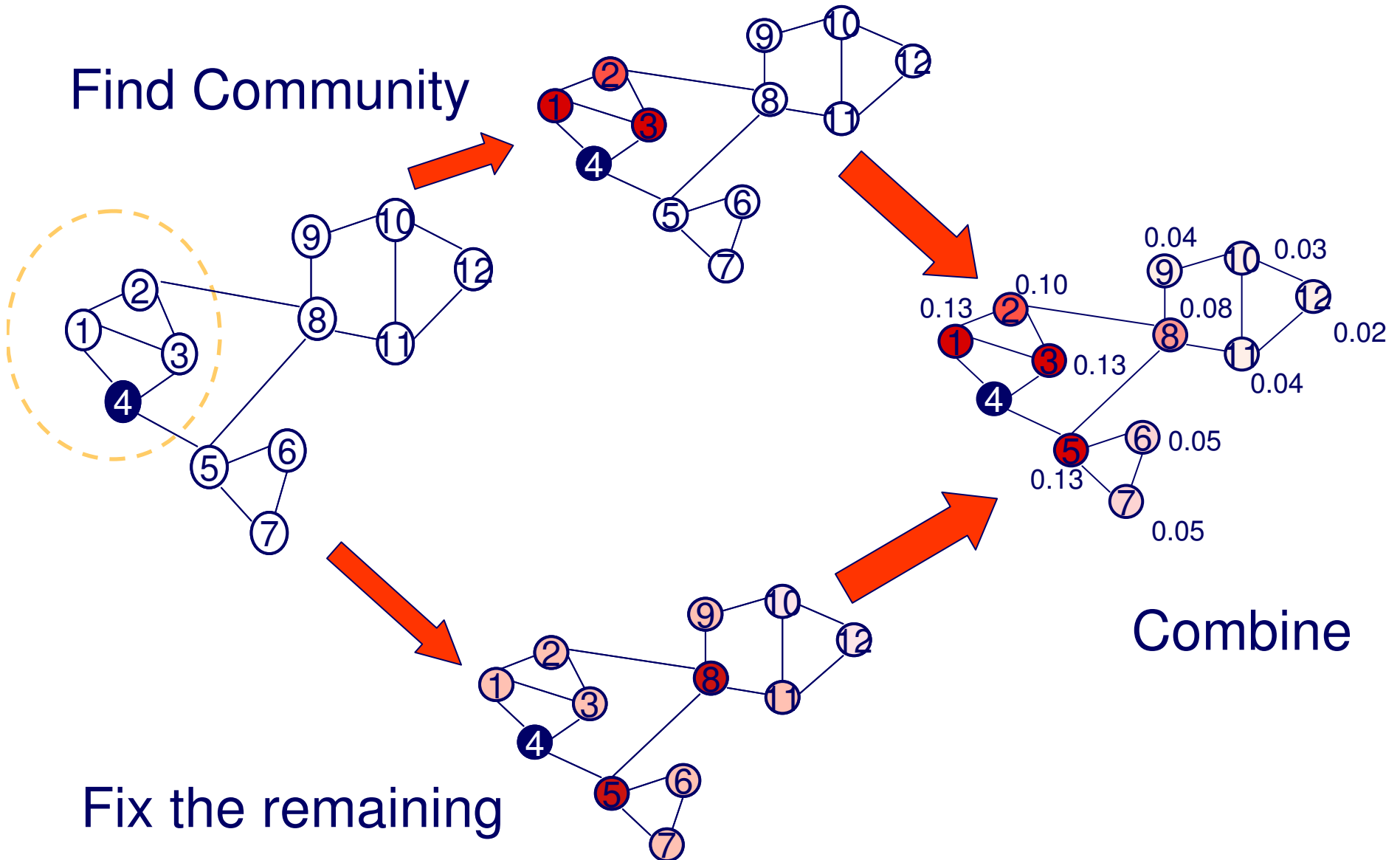
H. Tong, C. Faloutsos, & J.Y. Pan. *Fast Random Walk with Restart and Its Applications*. ICDM, 613-622, 2006.



B_Lin: Basic Idea

[Tong+ ICDM 2006]

Find Community





B_Lin: details

$$\tilde{W} \approx \underbrace{\begin{bmatrix} \tilde{W}_{11} & & \\ & \tilde{W}_{12} & \\ & & \tilde{W}_{13} \end{bmatrix}}_{\tilde{W}_1: \text{within community}} + \underbrace{\begin{bmatrix} U & S & V \end{bmatrix}}_{\text{Cross-community}}$$

The diagram illustrates the B_Lin model structure. It shows the approximation of the adjacency matrix \tilde{W} as the sum of two components. The first component, \tilde{W}_1 , represents within-community interactions and is shown as a block-diagonal matrix with blocks \tilde{W}_{11} , \tilde{W}_{12} , and \tilde{W}_{13} . The second component represents cross-community interactions and is shown as a matrix with columns U , S , and V .



B_Lin: details



$$\left(\mathbf{I} - c\tilde{\mathbf{W}} \right)^{-1} \approx \left(\underbrace{\left[\mathbf{I} - c\tilde{\mathbf{W}}_1 \right]}_{\text{Easy to be inverted}} - \underbrace{\left[c\mathbf{U}\mathbf{S}\mathbf{V} \right]}_{\text{LRA difference}} \right)^{-1}$$

Easy to be inverted LRA difference

SM Lemma!

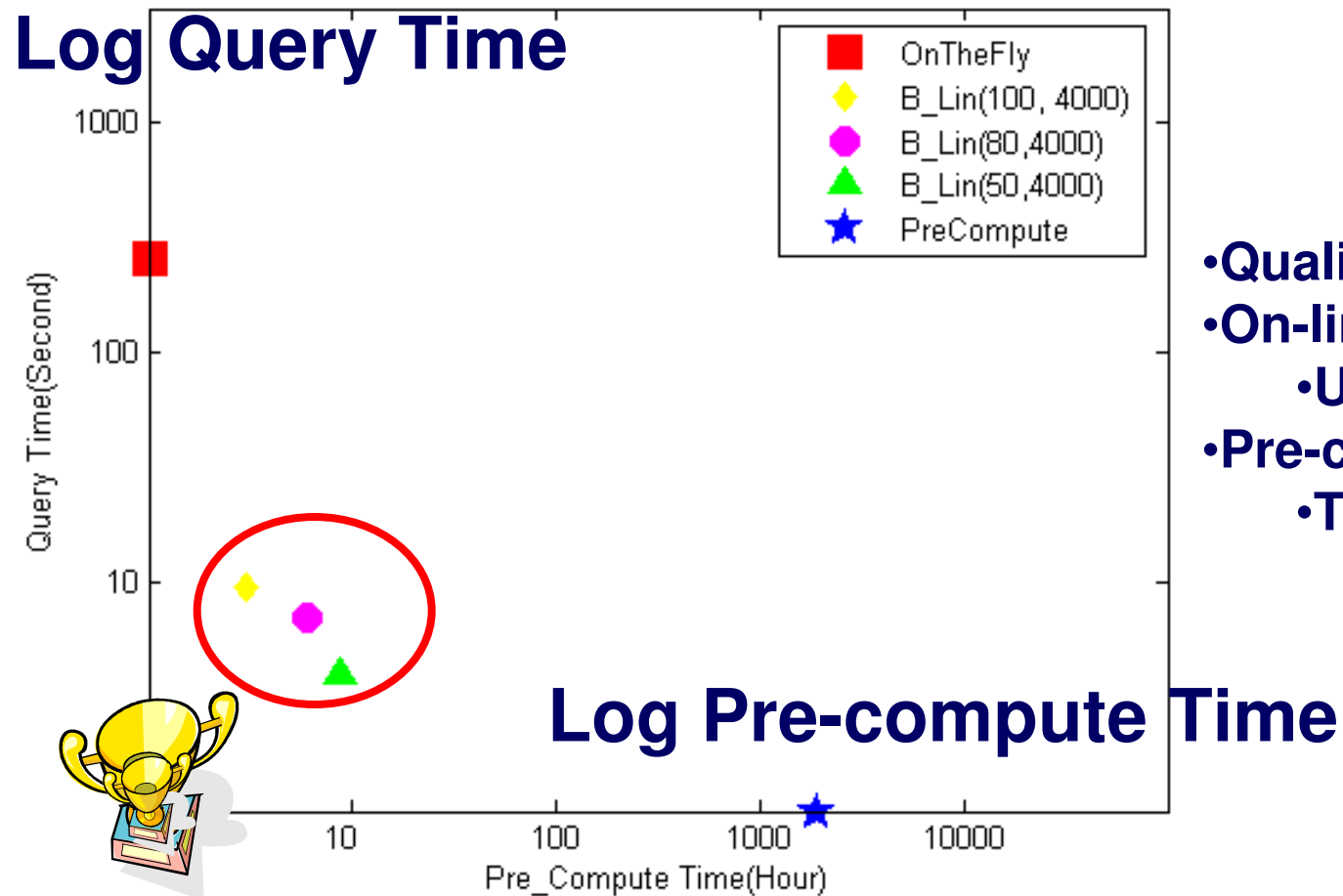


B_Lin: summary

- Pre-Computational Stage 
 - Q: Efficiently compute and store Q
 - A: A few small, instead of ONE BIG, matrices inversions
- On-Line Stage 
 - Q: Efficiently recover one column of Q
 - A: A few, instead of MANY, matrix-vector multiplications



Query Time vs. Pre-Compute Time



- Quality: 90%+
- On-line:
 - Up to 150x speedup
- Pre-computation:
 - Two orders saving



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gCaP: Automatic Image Caption

• Q



{Sea Sun Sky Wave}

...



{Cat Forest Grass Tiger}



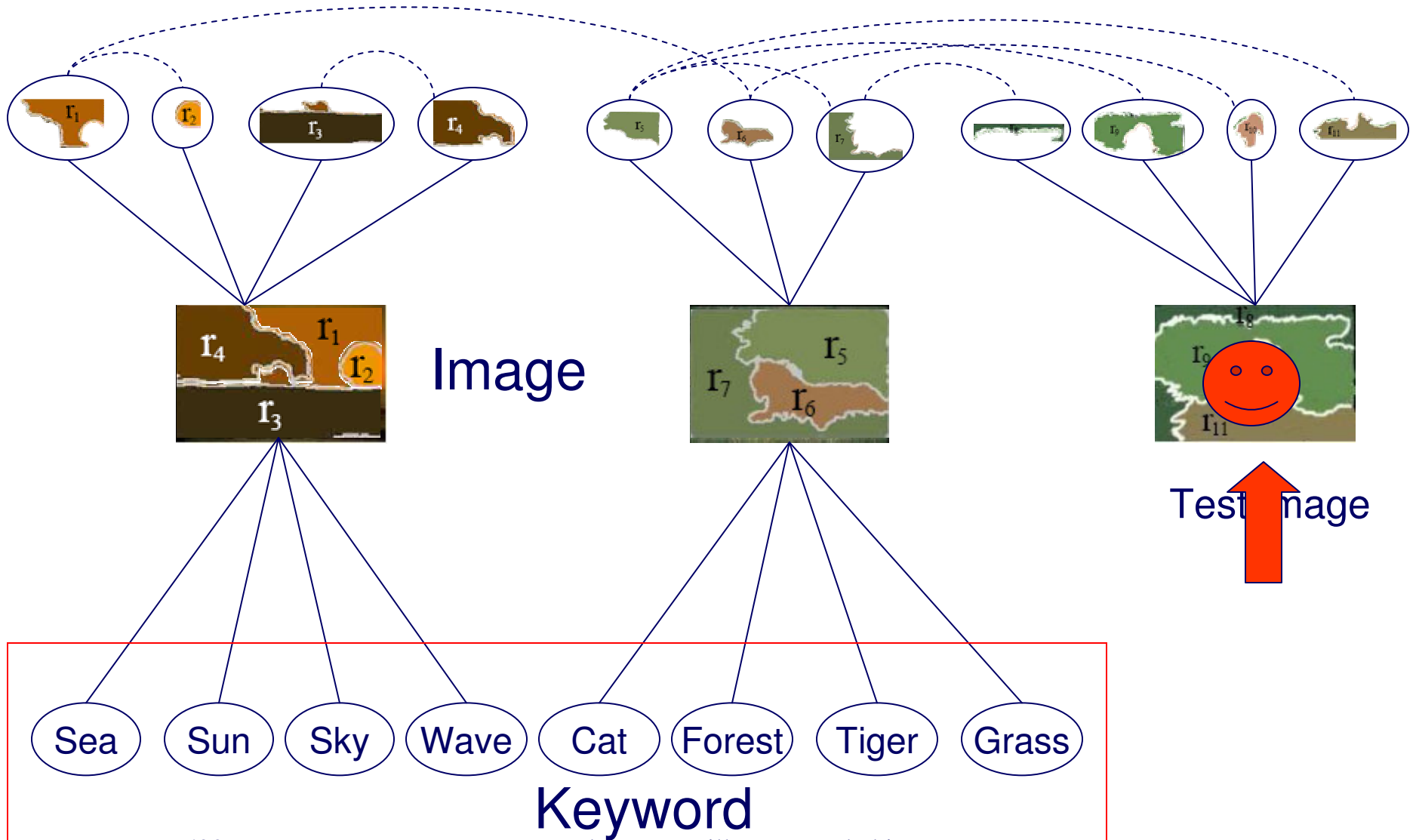
{?, ?, ?,}

A: Proximity!

[Pan+ KDD2004]

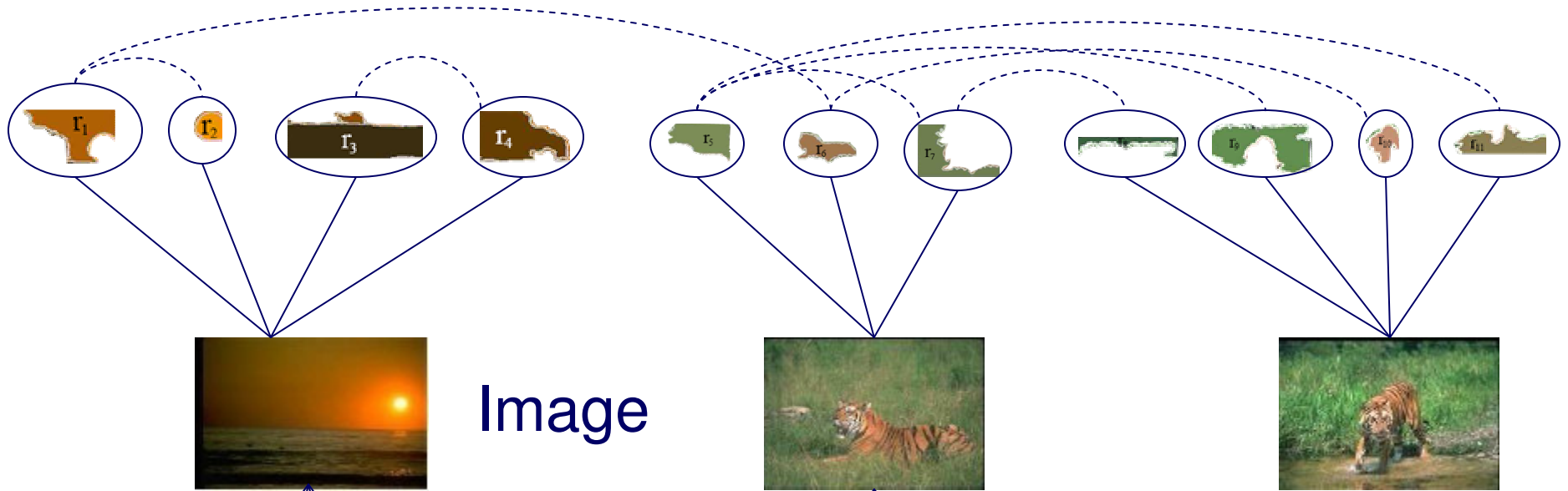


Region



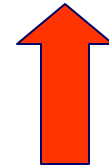


Region

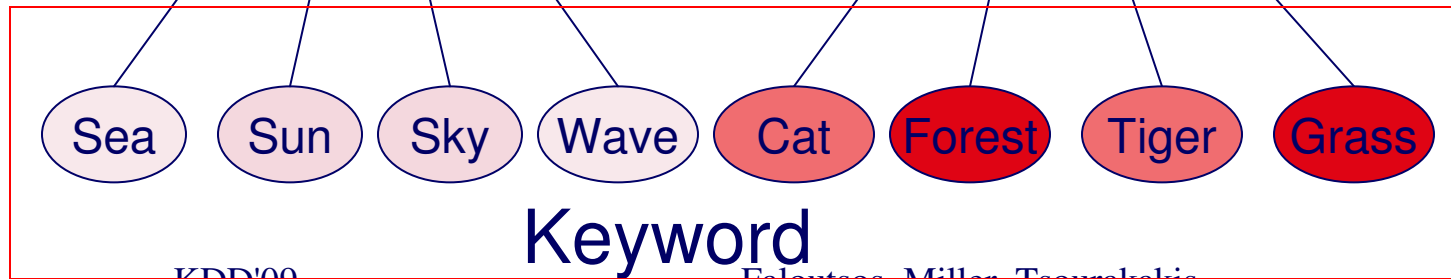


Image

{Grass, Forest, Cat, Tiger}

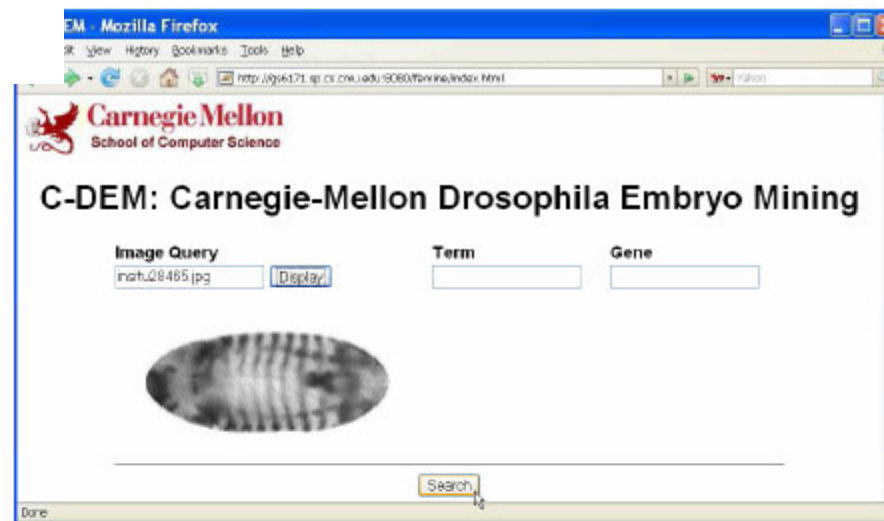


Keyword

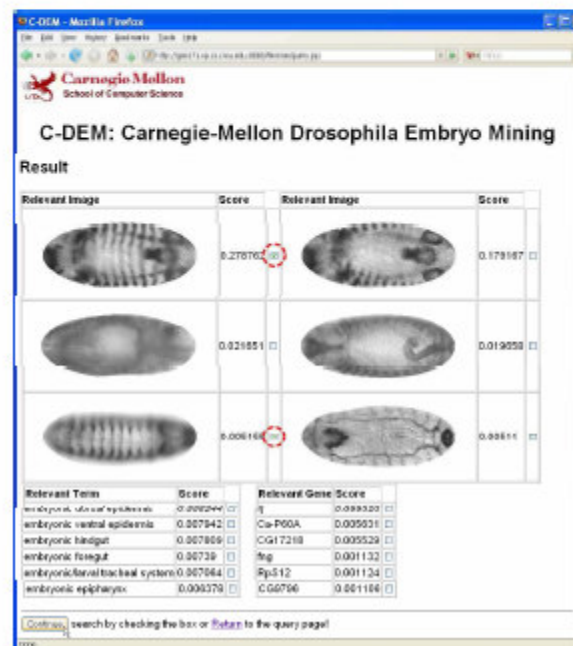


C-DEM (Screen-shot)

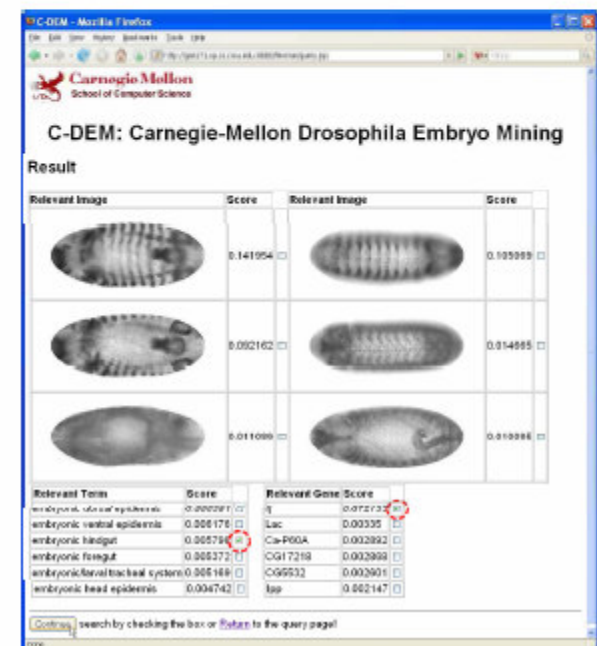
details



(a)



(b)

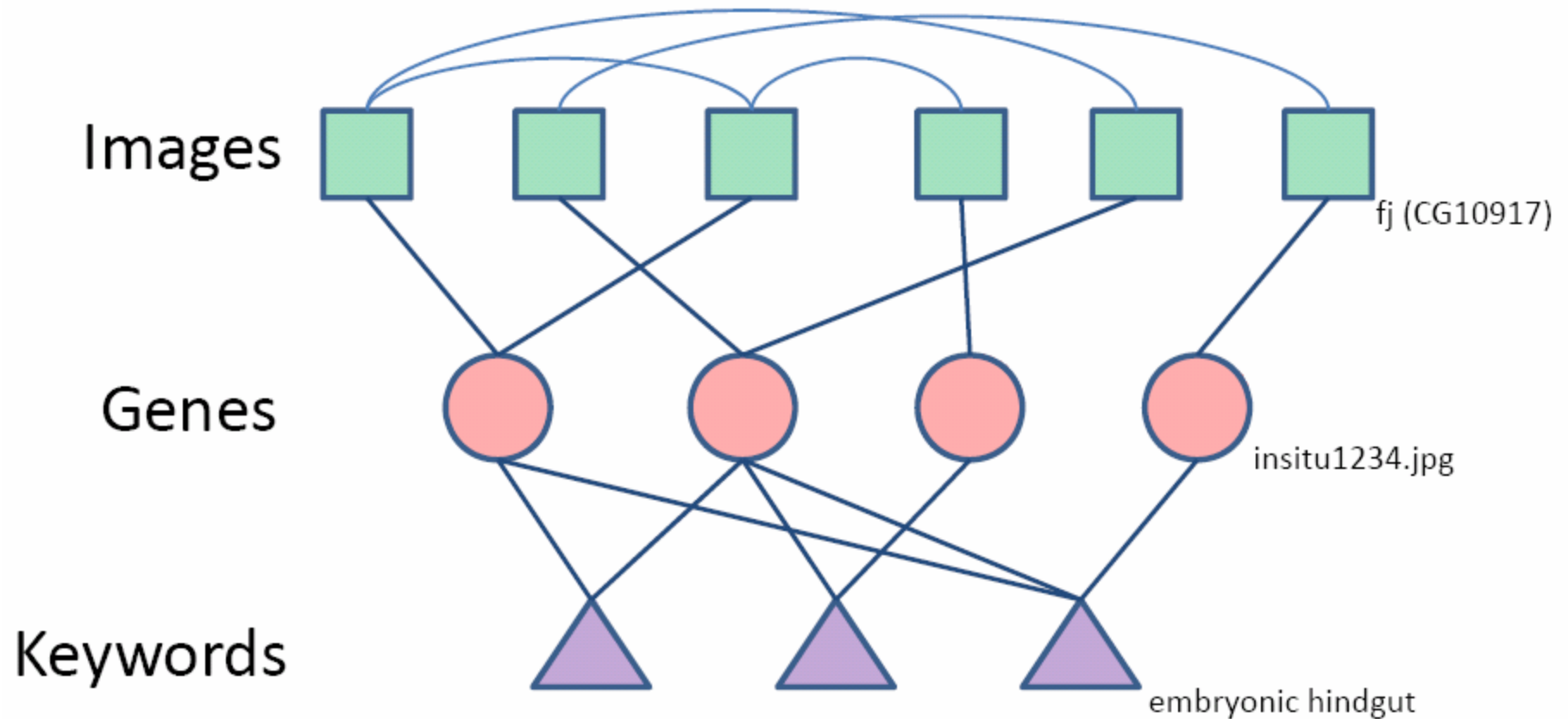


(c)



C-DEM: Multi-Modal Query System for Drosophila Embryo Databases [Fan+ VLDB 2008]

details





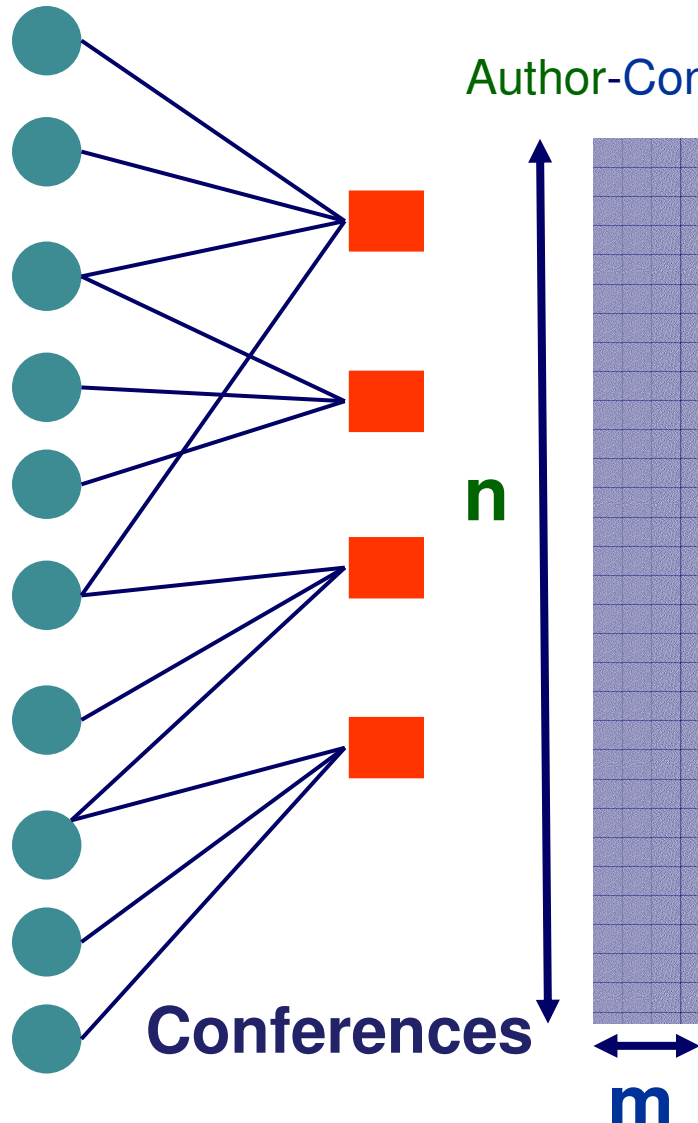
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authors

RWR on Bipartite Graph



Author-Conf. Matrix

Observation: $n \gg m$!

Examples:

1. DBLP: 400k aus, 3.5k confs
2. NetFlix: 2.7M usrs, 18k mvs

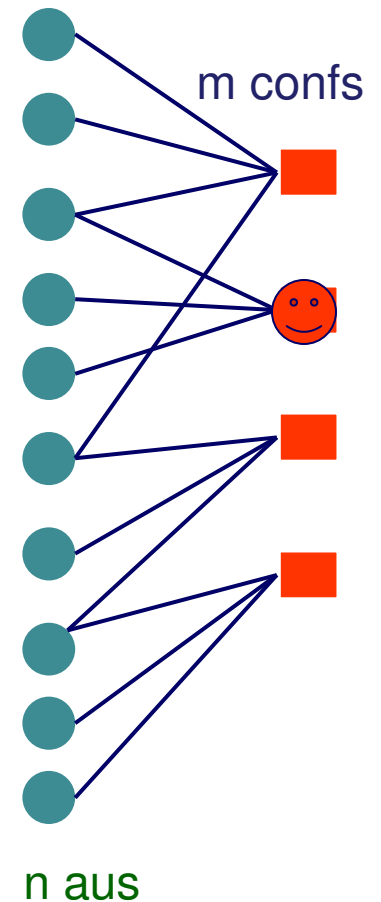


RWR on Skewed bipartite graphs

- Q: Given query i , how to solve it?

$$\begin{pmatrix} ? \\ \vdots \\ ? \end{pmatrix} = 0.9 \times \begin{pmatrix} 0 & \cdots & 0 \\ \vdots & \ddots & \vdots \\ 0 & \cdots & 0 \\ \vdots & \ddots & \vdots \\ 0 & \cdots & 0 \\ \vdots & \ddots & \vdots \\ 0 & \cdots & 0 \\ \vdots & \ddots & \vdots \\ 1/3 & \cdots & 0 \\ \vdots & \ddots & \vdots \\ 3 & \cdots & 0 \\ \vdots & \ddots & \vdots \\ 1/3 & \cdots & 1/2 \end{pmatrix} \begin{pmatrix} ? \\ \vdots \\ ? \end{pmatrix} + 0.1 \times \begin{pmatrix} 0 \\ 0 \\ 0 \\ 0 \\ 1 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \end{pmatrix}$$

$\underbrace{\hspace{15em}}_n \quad \underbrace{\hspace{5em}}_m$





Idea:

- Pre-compute the smallest, $m \times m$ matrix
- Use it to compute the rest proximities, on the fly

H. Tong, S. Papadimitriou, P.S. Yu & C. Faloutsos. *Proximity Tracking on Time-Evolving Bipartite Graphs*. SDM 2008.



BB_Lin: Examples

Dataset	Off-Line Cost	On-Line Cost
DBLP	a few minutes	frac. of sec.
NetFlix	1.5 hours	<0.01 sec.

400k authors
x 3.5k conf.s

2.7m user
x 18k movies



Detailed outline

- Problem defn and motivation
- Solution: Random walk with restarts
- Efficient computation
- Case study: image auto-captioning
- ➔ • Extensions: bi-partite graphs; **tracking**
- Conclusions



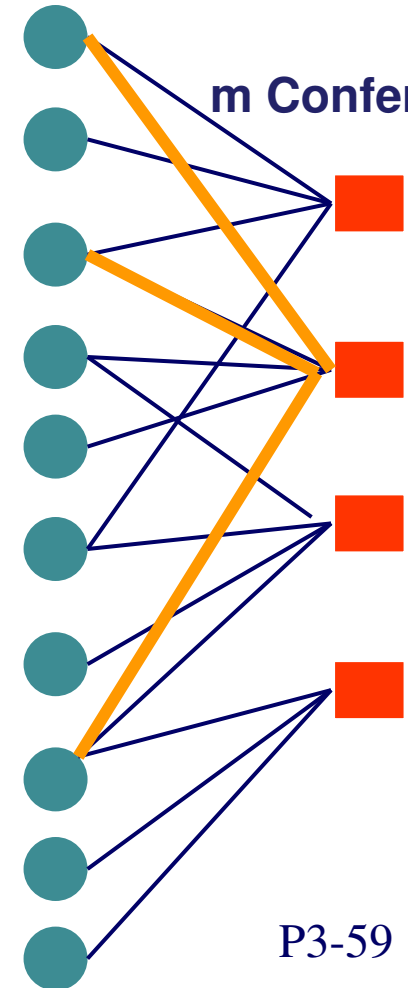
Problem: update

E' edges changed

Involves n' authors, m' confs.

n authors

m Conferences



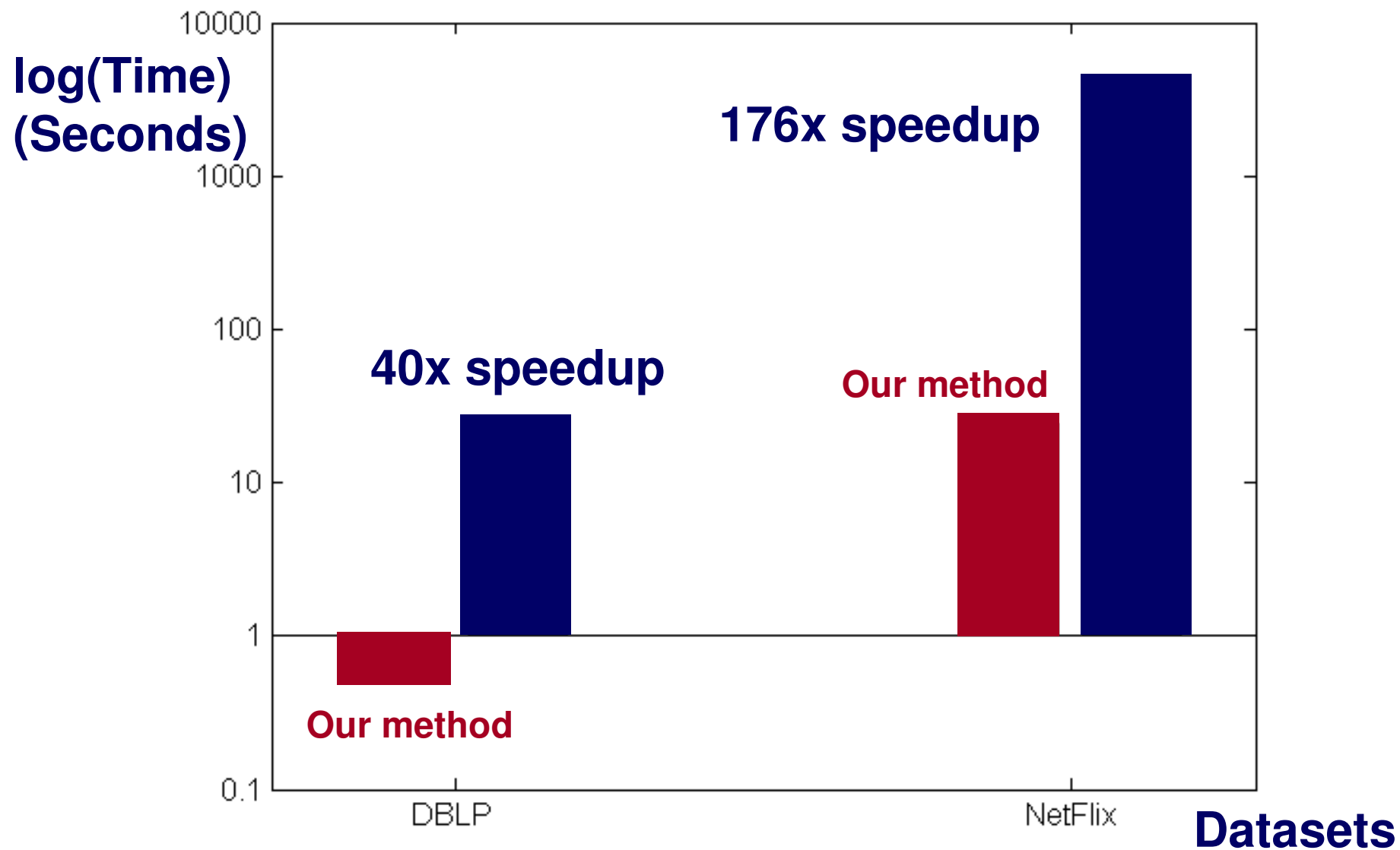


Solution:

- Use Sherman-Morrison to quickly update the inverse matrix



Fast-Single-Update





pTrack: Philip S. Yu's Top 5 conferences up to each year

ICDE ICDCS SIGMETRICS PDIS VLDB	CIKM ICDCS ICDE SIGMETRICS ICMCS	KDD SIGMOD ICDM CIKM ICDCS	ICDM KDD ICDE SDM VLDB
1992	1997	2002	2007

DBLP: (Au. x Conf.)

- 400k aus,
- 3.5k confs
- 20 yrs



pTrack: Philip S. Yu's Top 5 conferences up to each year

ICDE ICDCS SIGMETRICS PDIS VLDB	CIKM ICDCS ICDE SIGMETRICS ICMCS	KDD SIGMOD ICDM CIKM ICDCS	ICDM KDD ICDE SDM VLDB
1992	1997	2002	2007



Databases
Performance
Distributed Sys.

KDD'09

DBLP: (Au. x Conf.)

- 400k aus,
- 3.5k confs
- 20 yrs

Faloutsos, Miller, Tsourakakis

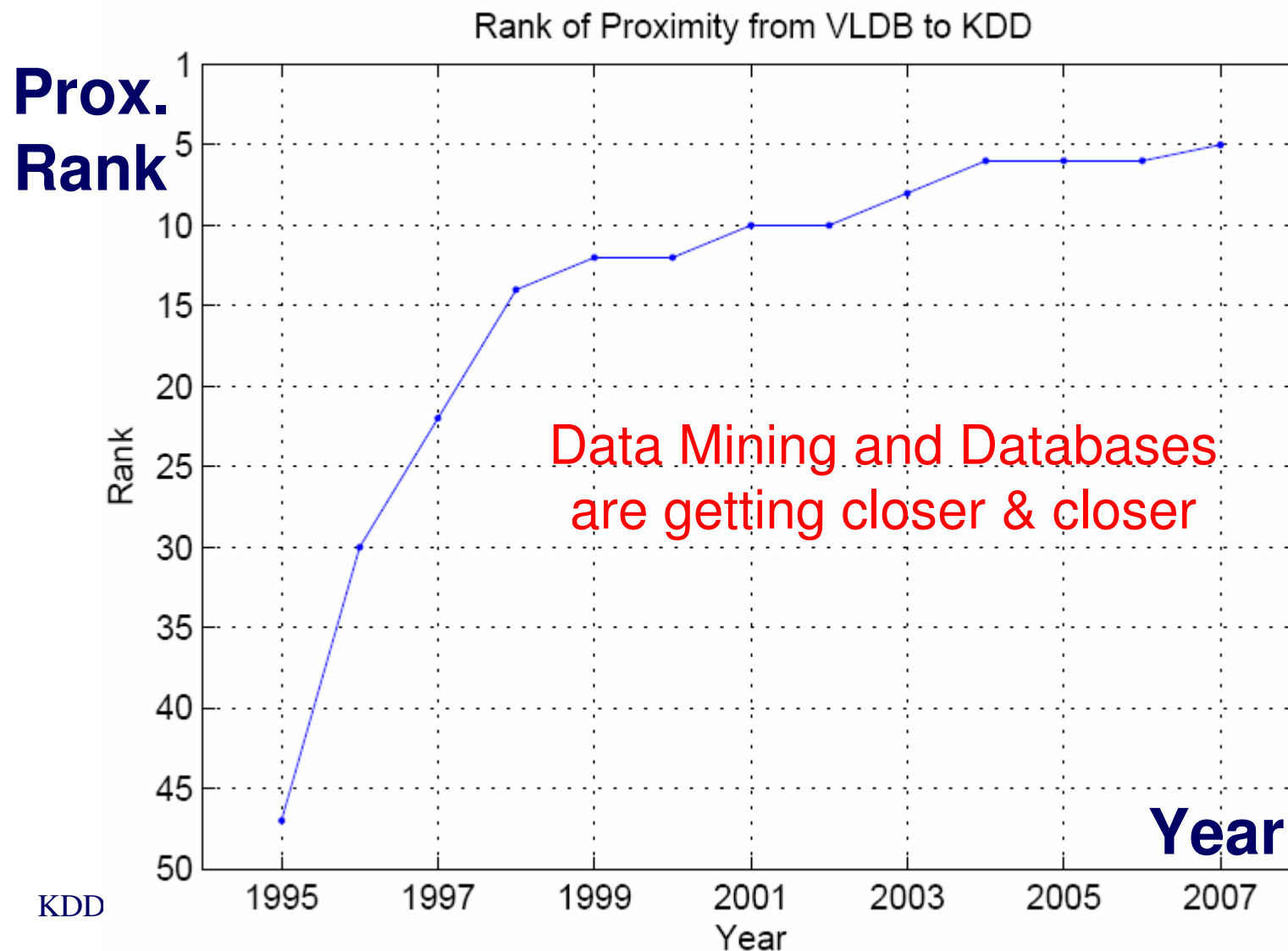


Databases
Data Mining

P3-63



KDD's Rank wrt. VLDB over years





cTrack:10 most influential authors in NIPS community up to each year

T. Sejnowski

1987	1989	1991	1993	1995	1997	1999
'Abbott_L'	'Bower_J'	'Hinton_G'	'Sejnowski_T'	'Sejnowski_T'	'Sejnowski_T'	'Sejnowski_T'
'Burr_D'	'Hinton_G'	'Koch_C'	'Koch_C'	'Jordan_M'	'Jordan_M'	'Koch_C'
'Denker_J'	'Tesauro_G'	'Bower_J'	'Hinton_G'	'Hinton_G'	'Koch_C'	'Jordan_M'
'Schofield_C'	'Denker_J'	'Sejnowski_T'	'Mozier_M'	'Koch_C'	'Hinton_G'	'Hinton_G'
'Bower_J'	'Mead_C'	'LeCun_Y'	'LeCun_Y'	'Mozier_M'	'Mozier_M'	'Mozier_M'
'Brown_N'	'Tenorio_M'	'Mozier_M'	'Denker_J'	'Bengio_Y'	'Dayan_P'	'Dayan_P'
'Carley_L'	'Sejnowski_T'	'Denker_J'	'Bower_J'	'Lippmann_R'	'Bengio_Y'	'Singh_S'
'Chou_P'	'Lippmann_R'	'Waibel_A'	'Kawato_M'	'LeCun_Y'	'Barto_A'	'Bengio_Y'
'Chover_J'	'Touretzky_D'	'Moody_J'	'Waibel_A'	'Waibel_A'	'Tresp_V'	'Tresp_V'
'Eeckman_F'	'Koch_C'	'Lippmann_R'	'Simard_P'	'Simard_P'	'Moody_J'	'Moody_J'

M. Jordan

Author-paper bipartite graph from NIPS 1987-1999.

3k. 1740 papers, 2037 authors, spreading over 13 years



Conclusions - Take-home messages

- **Proximity Definitions**

- RWR $\vec{r}_i = c\tilde{W}\vec{r}_i + (1 - c)\vec{e}_i$
- and a lot of variants

- **Computation**

- Sherman–Morrison Lemma
- Fast Incremental Computation

- **Applications**

- Recommendations; auto-captioning; tracking
- Center-piece Subgraphs (next)
- E-mail management; anomaly detection, ...



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- H. Tong, H. Qu, and H. Jamjoom. Measuring Proximity on Graphs with Side Information. ICDM 2008



Resources

- www.cs.cmu.edu/~htong/soft.htm
For software, papers, and ppt of presentations
- www.cs.cmu.edu/~htong/tut/cikm2008/cikm_tutorial.html
For the CIKM'08 tutorial on graphs and proximity



Again, thanks to **Hanghang TONG**
for permission to use his foils in this
part