

Graduate Aerospace Laboratories Kochmann Research Group

# Non-linear Homogenization using Spectral Methods: Applications to Crystal Plasticity and Electromechanical Microstructures

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#### 01 | Theory

## Multi-scale modeling using homogenization

- Analytical and computational study of large and complex systems involves multi-scale analysis, particularly so in micromechanics of materials
- Subsequently, numerical homogenization is a tool that provides a means of scale bridging for systems with statistically homogeneous or periodic lower scale structure, which commonly arises in mechanics of materials
- Fourier spectral methods are versatile quasi-linear scaling techniques, useful for periodic numerical homogenization
- Techniques of mitigating non-uniform convergence of Fourier spectral methods for nonlinear problems with lack of smoothness and complex microstructure
  - Modified Green's operator, spectral re-projection
- Application of numerical homogenization to selected material modelling problems which span scales, governed by elliptic equations with multiscale coefficients
  - Crystal plasticity of HCP metals
  - Electromechanical coupling in Ferroelectric ceramics