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## Index of Special Notations

		$\operatorname{Sec}$	tion	Pag	ge
$S \subset T$	(S  is a subset of  T)		01		3
$S \subsetneq T$	(S  is a proper subset of  T)		01		3
$S \setminus \overline{T}$	(set-difference of $S$ and $T$ )		01		4
$(a_i \mid i \in I)$	(family with index set $I$ )		02		7
$S^{I}$	(set of all families in $S$ with index set $I$ )		02		$\overline{7}$
$M^{(I)}$	(set of all families in $M$ with index				
	set $I$ and finite support)		07		28
$(\mathbb{R}^{(I)})_{\nu}$	(set of all families in $\mathbb{R}$				
	with index set $I$ , finite support, and sum $\nu$ )	35,	37	116	5,124
$X(A_i i \in I$	)(set-product of the family $(A_i   i \in I)$ of sets)		04		15
$f \times g$	(cross-product of the mappings $f$ and $g$ )		04		17
$X\left(f_{i} i\in I\right)$	(cross-product of the family $(f_i   i \in I)$				
	of mappings)		04		17
$g^{ imes I}$	(I-cross-power of the mapping $g$ )		04		18
$f_{>}$	(image mapping of $f$ )		03		12
$f^{<}$	(pre-image mapping of $f$ )		03		12
$f^{\leftarrow}$	(inverse of the mapping $f$ )		03		11
$f^{\circ n}$	(n th iterate of the mapping  f)		03		11
$f _A$	(restriction of $f$ to $A$ )		03		12
$f _A^B$	(adjustment of $f$ range)		03		12
$f ^{\mathrm{Rng}}$	(adjustment of $f$ to range)		03		13
$f_{ A }$	(A-adjustment of $f$ when $A$ is $f$ -invariant)		03		13
$f_{(\mathcal{V})}$	(lineonic extension of $f$ )		85		316
$c_{D \to C}$	(constant with domain $D$ , codomain $C$ , and				
	range $\{c\}$ )		03		11
$1_S$	(identity mapping of $S$ )		03		11
$1_{U \subset S}$	(inclusion mapping of $U$ into $S$ )		03		11
$(a, \cdot), (\cdot, b)$	("insertion" into a product of two sets)		04		18
(c.j)	("insertion" into a product of a family of sets)		04		19
$\sharp S$	(cardinal of $S$ )		05		20
[x,y]	(closed interval; segment joining the points $x$				
	and $y$ )	08,	37	32,	123
]x,y[	(open interval; open segment joining the				
	points $x$ and $y$ )	08,	51	32,	163

		Sect	ion	Page
[a,b[,]a,b]	(half-open intervals)		08	31
$\mathbb{R}$	(extended-real-number set)		08	32
$\mathbb{P}$	(extended-positive-number set)		08	32
ι	(identity-mapping of $\mathbb{R}$ ; "indeterminate")	08,	92	34, 353
$\partial_t f$	(derivative of $f$ at $t$ )	08,	61	34, 209
$\partial f$	(derivative-function of $f$ )	08,	61	34, 209
$f^{ullet}$	(derivative-function of $f$ )	08,	61	35, 210
$\partial^n f, f^{(n)}$	(derivative of order $n$ )	08,	61	35, 209
$\nabla$	(gradient)	33,	63	108, 218
$\nabla_{(1)}, \nabla_{(2)}$	(partial gradients)		65	228, 229
$\varphi_{,1}, \varphi_{,2}$	(partial derivatives)		65	228, 229
$\nabla_{(j)}, \varphi_{,j}$	(partial gradients and derivatives)		65	231
$\triangle$	(Laplacian)		67	241
$\mathbf{L}_1 \oplus \mathbf{L}_2$	("evaluation-sum" of $\mathbf{L}_1$ and $\mathbf{L}_2$ )		14	49
$\bigoplus(\mathbf{L}_i i \in I)$	("evaluation-sum" of a family of			
	linear mappings)		14	50
$\delta^{I}$	(standard basis of $\mathbb{F}^{(I)}$ )		16	55
$\mathcal{V}^*$	(dual of the linear space $\mathcal{V}$ )		21	71
$\mathbf{b}^*$	(dual of the basis $\mathbf{b}$ )		23	78
$\mathbf{L}^\top$	$(\text{transpose of the linear mapping } \mathbf{L})$	21	71	
$\mathcal{S}^{\perp}$	(annihilator of the set $\mathcal{S}$ ; orthogonal supplement)	21, 4	41,	$72,\!137$
$\mathbf{B}^{\sim}$	(switch of the bilinear mapping $\mathbf{B}$ )		24	83
$\mathbf{w}\otimesoldsymbol{\lambda}$	(tensor product of $\mathbf{w}$ and $\boldsymbol{\lambda}$ )		25	86
$\overline{\mathbf{S}}$	(quadratic form corresponding to the			
	bilinear form $\mathbf{S}$ )		27	94
$\overline{\mathbf{Q}}$	(bilinear form corresponding to the			
	quadratic form $\mathbf{Q}$ )		28	94
$\overleftrightarrow{xy}$	(line passing through the points $x$ and $y$ )		32	107
$\mathbf{v}^{\cdot 2}$	(inner square of $\mathbf{v}$ )		41	133
$\mathbf{u}\cdot\mathbf{v}$	(inner product of $\mathbf{u}$ and $\mathbf{v}$ )		41	133
$\langle {f u}   {f v}  angle$	(unitary product of $\mathbf{u}$ and $\mathbf{v}$ )		89	337
$ \mathbf{v} $	(magnitude of $\mathbf{v}$ )		42	139
$  \mathbf{L}  _{ u, u'}$	(operator norm of <b>L</b> relative to $\nu, \nu'$ )		52	174
$  \mathbf{L}  _{ u}$	(operator norm of the line on ${\bf L}$ relative to $\nu)$		52	174
$  \mathbf{L}  $	(operator norm of <b>L</b> relative to magnitude)		52	176
$[\mathbf{L}]_{\mathbf{b}}$	(matrix of the lineon $\mathbf{L}$ relative to the basis $\mathbf{b}$ )		18	63
$[\mathbf{h}]^c, [\mathbf{h}]_c, [\mathbf{T}]^c{}_d$	(components relative to a coordinate system)	71,	73	279,289

# Index of Multiple-Letter Symbols

		Section	Page
Acc	(set of accumulation points, of a set)	57	197
add	(addition mapping)	11	39
Aspec	(angle-spectrum, of a lineon)	88	333
Asps	(angle-spectral space, of a lineon)	88	333
Ball	(ball, in a genuine Euclidean space)	46	153
Bdy	(boundary, of a set)	53	179
Box	(norming box, determined by a basis)	51	168
Ce	(Norming cell, of a norm)	51	164
$^{\mathrm{ch}}$	(characteristic family or function, of a set)	$02, \ 03$	8, 10
$^{\mathrm{chp}}$	(characteristic polynomial, of a lineon)	95	370
Clo	(closure, of a set)	53	178
Cod	(codomain, of a mapping)	03	9
Comm	(commutant algebra, of a lineon)	18	62
Conf	(set of confined mappings)	62	213, 216
Curl	(curl, of a mapping)	611	261
cxc	(convex-combination mapping, of a family in a		
	flat space)	37	124
Cxh	(convex hull, of a subset of a flat space)	37	123
dd	(directional derivative)	65	233
$\operatorname{deg}$	(degree, of a polynomial)	92	353
$\det$	(determinant)	73	287
diam	(diameter)	52	173
diff	(point-difference mapping)	32	103
$\dim$	(dimension, of a linear space or a flat space)	17, 32	58, 107
div	(divergence)	67	239
Dmd	(norming diamond, determined by a basis)	51	168
Dom	(domain, of a mapping)	03	9
$\operatorname{dst}$	(distance function, of a genuine Euclidean space)	46	152
Eis	(group of Euclidean automorphisms)	45	149
$\operatorname{emult}$	(elementary multiplicity function, of a lineon)	95	370
ev	(evaluation, on a set-product or a set of mappings)	04, 22,	16,17,74

		Sec	tion	Pag	ge	
$\exp$	(exponential, lineonic exponential)	08,	612	2  34,	266	
Fin	(set of all finite subsets, of a set)		05		21	
Fis	(group of flat automorphisms)		33		111	
flc	(flat combination mapping, of a family in a flat space)		35		116	
$\operatorname{Flf}$	(space of flat functions)		36		120	
$\operatorname{Fsp}$	(flat span, of a subset of a flat space)		32		107	
$\operatorname{Gr}$	(graph, of a mapping)		03		10	
ind	(index, of an inner-product space)		47		157	
Inj	(set of all injective mappings from a given set					
	to another)		04		16	
$\inf$	(infinum, of a set)		08		32	
ins	(insertion mapping)	14,	15	48,	52	
Int	(interior, of a set)		53		177	
inv	(inversion mapping)		68		246	
ip	(inner-product)		41		133	
Ker	(kernel, of a homomorphism)		06		24	
lim	(limit)	08,	55,	57 34,	186, 19	98
Lin	(space of linear mappings, from a given linear space					
	to another; algebra of lineons)	14,	18	47,	61	
$Lin_2$	(space of bilinear mappings)		24		81	
Lis	(set of linear isomorphism, from a given linear space					
	to another; linear group)	14,	18	48,	62	
lnc	(linear combination mapping, of a family in a					
	linear space)		15		51	
log	(lineonic logarithm)		85		320	
lp	(polar decomposition, left positive part)		86		324	
Lsp	(linear span, of a subset of a linear space)	12,	92	42,	355	
Map	(set of all mappings, from a given set to another)		04		16	
max	(maximum, of a set)		08		32	
$\min$	(minimum, of a set)		08		32	
mult	(multiplicity function, of a lineon)	82,	81(	) 307	,340	
Nhd	(collection of neighborhoods, of a point)	,	53		177	

### $Index \ of \ Multiple-Letter \ Symbols$

		$\operatorname{Sec}$	tion	$Pa_{2}$	ge
no	(norm, of a norming cell)		51		165
Null	(nullspace, of a linear mapping)		13		46
opp	(opposition mapping)		11		39
or	(polar decomposition, orthogonal part)		86		324
Orth	(set of orthogonal mappings, from a given				
	inner-product space to another; orthogonal group)		43	141	1,142
Perm	(set of all permutations, of a given set)		04		16
Pos	(set of positive symmetric lineons)		85		316
$\operatorname{Pos}^+$	(set of strictly positive symmetric lineons)		85		316
pow	(lineonic power)		66		237
Pspec	(pair-spectrum, of a lineon)		88		330
$\mathbf{Psps}$	(pair-spectral space, of a lineon)		88		330
${ m Qu}$	(space of quadratic forms)		27		94
Qspec	(quasi-spectrum, of a lineon)		87		327
Qsps	(quasi-spectral space, of a lineon)		87		327
Rng	(range, of a family or a mapping)	02,	03	7,	10
rp	(polar decomposition, right positive part)		86		324
$\operatorname{sep}$	(separation function, of a Euclidean space)		45		148
$\operatorname{sgn}$	(sign-function)		08		32
$\operatorname{sig}$	(signature, of an inner-product space)		47		155
Skew	(space of skew linear mappings or lineons)	27,	41	92,	135
$\operatorname{Skew}_2$	(space of skew bilinear mappings)		24		83
$\mathrm{sm}$	(scalar-multiple mapping)	11,	89	39,	335
$\operatorname{Small}$	(set of small mappings)		62	212	2,216
$\operatorname{Spec}$	(spectrum, of a lineon)	82,	810	307	7,340
$\operatorname{Sph}$	(sphere, in a genuine Euclidean space)		46		153
$\operatorname{Sps}$	(spectral space, of a lineon)	82,	810	307	7,340
$\mathbf{sq}$	(inner square)		41		133
$\operatorname{sqrt}$	(lineonic square root)		85		317
$\mathrm{sqrt}^+$	(strict lineonic square root)		85		318
$\operatorname{ssq}$	(sum-sequence, of a sequence)	08,	55	33,	191
$\operatorname{str}$	(striction, of a mapping relative to given norms;				
	absolute striction)		64	223	3,227

### $Index \ of \ Multiple-Letter \ Symbols$

		Section	Page
Sub	(subsetset, of a set)	01	3
sum	(summation mapping)	15	51
sup	(supremum of a set)	08	32
Supt	(support, of a family)	07	28
Sym	(space of symmetric linear mappings or lineons)	27, 41	92, 135
$\operatorname{Sym}_2$	(space of symmetric bilinear mappings)	24	83
tr	(trace, of a lineon)	26	89
Ubl	(unit ball, in a genuine inner-product space)	42	140
Unit	(set of unitary mappings, from a given unitary		
	space to another; unitary group)	89	339
Usph	(unit sphere, in a genuine inner-product space)	42	140

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