

# Math 241 Homework

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Complete the following problems. Fully justify each response.

1. Calculate each of the following determinants:

(a)  $\det \left( \begin{bmatrix} 2 & 3 \\ -1 & 1 \end{bmatrix} \right)$

(b)  $\det \left( \begin{bmatrix} 1 & 2 & -1 \\ 2 & 1 & 0 \\ 0 & 1 & 0 \end{bmatrix} \right)$

2. Prove that the determinant of an upper triangular matrix is equal to the product of the diagonal entries of the matrix.
3. Complete problems 12.14.2, 12.14.3, 12.14.9 on pages 483-485 in Coding the Matrix.
4. Suppose that  $\lambda$  is an eigenvalue of the invertible matrix  $A$  having a corresponding eigenvector  $\mathbf{v}$ . Prove that  $\frac{1}{\lambda}$  is an eigenvalue of  $A^{-1}$ . What is a corresponding eigenvector?
5. Use the previous problem to prove that a square matrix  $A$  is invertible if and only if 0 is not an eigenvalue of  $A$ .
6. Complete the problem set found at [autolab.andrew.cmu.edu](http://autolab.andrew.cmu.edu). The submission for this is directly on autolab, no need to hand it in on paper.