## Putnam S.11

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## 1 Problems

Putnam 1999/A4. Sum the series

$$\sum_{m=1}^{\infty} \sum_{n=1}^{\infty} \frac{m^2 n}{3^m (n3^m + m3^n)}.$$

**Putnam 1999/A5.** Prove that there is a constant C such that, if p(x) is a polynomial of degree 1999, then

$$|p(0)| \le C \int_{-1}^{1} |p(x)| dx.$$

**Putnam 1999/A6.** The sequence  $(a_n)_{n\geq 1}$  is defined by  $a_1 = 1, a_2 = 2, a_3 = 24, \text{ and, for } n \geq 4,$ 

$$a_n = \frac{6a_{n-1}^2 a_{n-3} - 8a_{n-1}a_{n-2}^2}{a_{n-2}a_{n-3}}.$$

Show that, for all n,  $a_n$  is an integer multiple of n.