Putnam E.09

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1 Problems

- **Putnam 2002/A1.** Let k be a fixed positive integer. The *n*-th derivative of $\frac{1}{x^{k}-1}$ has the form $\frac{P_{n}(x)}{(x^{k}-1)^{n+1}}$ where $P_{n}(x)$ is a polynomial. Find $P_{n}(1)$.
- **Putnam 2002/A2.** Given any five points on a sphere, show that some four of them must lie on a closed hemisphere.
- **Putnam 2002/A3.** Let $n \ge 2$ be an integer and T_n be the number of non-empty subsets S of $\{1, 2, 3, \ldots, n\}$ with the property that the average of the elements of S is an integer. Prove that $T_n n$ is always even.