Putnam E.05

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1 Problems

- **Putnam 2000/A1.** Let A be a positive real number. What are the possible values of $\sum_{j=0}^{\infty} x_j^2$, given that x_0, x_1, \ldots are positive numbers for which $\sum_{j=0}^{\infty} x_j = A$?
- **Putnam 2000/A2.** Prove that there exist infinitely many integers n such that n, n + 1, n + 2 are each the sum of the squares of two integers. [Example: $0 = 0^2 + 0^2$, $1 = 0^2 + 1^2$, $2 = 1^2 + 1^2$.]
- **Putnam 2000/A3.** The octagon $P_1P_2P_3P_4P_5P_6P_7P_8$ is inscribed in a circle, with the vertices around the circumference in the given order. Given that the polygon $P_1P_3P_5P_7$ is a square of area 5, and the polygon $P_2P_4P_6P_8$ is a rectangle of area 4, find the maximum possible area of the octagon.