Putnam E.01

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1 Problems

Putnam 1998/B1. Find the minimum value of

$$\frac{(x+1/x)^6 - (x^6+1/x^6) - 2}{(x+1/x)^3 + (x^3+1/x^3)}$$

for x > 0.

- **Putnam 1998/B2.** Given a point (a, b) with 0 < b < a, determine the minimum perimeter of a triangle with one vertex at (a, b), one on the *x*-axis, and one on the line y = x. You may assume that a triangle of minimum perimeter exists.
- **Putnam 1998/B3.** Let *H* be the unit hemisphere $\{(x, y, z) : x^2 + y^2 + z^2 = 1, z \ge 0\}$, *C* the unit circle $\{(x, y, 0) : x^2 + y^2 = 1\}$, and *P* the regular pentagon inscribed in *C*. Determine the surface area of that portion of *H* lying over the planar region inside *P*, and write your answer in the form $A \sin \alpha + B \cos \beta$, where *A*, *B*, α , β are real numbers.