

Calculus I, 21-111
Review problems for the second test
March 26

1. Sketch the following curves:
 - (a) $y = x^3 - \frac{3}{2}x^2 - 6x$
 - (b) $y = x^4 - 4x^3$
2. Determine two numbers such that the product of one and the square of the other is 32, and their sum is as small as possible.
3. The demand curve for a product is given by $p = 50 - .2x$ and the cost of producing x units of the product is $C(x) = .1x^2 + 5x + 96$.
 - (a) What quantity of the product will yield the maximum profit?
 - (b) What will the selling price be at the quantity producing the maximum profit?
4. Mooncents Coffee sells freshly baked double chocolate cookies at a steady rate all day – a total of 144 a day. The manager wants to know how many cookies to make in each batch. Preparing a batch costs \$8 in employee time and it takes \$.25 worth of shelf space to store one cookie while awaiting sale. How many cookies should they make in each batch to minimize the cost in employee time and storage?
5. A farmer wants to fence a pasture at the intersection of two roads so that it will have a road along an end and a side. He also wants to partition it by a fence down the middle and parallel to one side. The fence next to a road costs \$8 a yard and the rest of the fence costs \$4 a yard. If the farmer has \$960 to spend on the fence what is the largest pasture he can make?
6. Find the point on the line $y = 4x + 5$ closest to the origin.
7. Let the functions f and g satisfy $f(2) = 4$, $f'(2) = 3$, $g(2) = -2$, and $g'(2) = 3$. Determine the value of each of the following:
 - (a) $\frac{d}{dx} \left(\frac{f(x)}{g(x)} \right)$ where $x = 2$.

(b) $\frac{d}{dx}(f(x)g(x))$ where $x = 2$.

8. Let the functions f and g satisfy $f(4) = 5$, $f'(4) = -3$, $g(2) = 4$, and $g'(2) = 3$. Determine the value of the following derivative where $x = 2$:

$$\frac{d}{dx}[f(g(x))]$$

9. Given the equation $x^2 - y^2 - xy = 5$, determine the slope of the tangent line to the graph at $(3, 1)$.
10. At noon, a ship is 100 km west of San Francisco. It sails due north at 30 km/hr. How fast is the distance from the ship to the city changing at noon? At 4 pm?