

2.5: 6. $Q = x^2 y$ $x + y = 2$

$\Rightarrow y = 2 - x$

so $Q = x^2(2 - x) = 2x^2 - x^3$

$Q' = 4x - 3x^2$

set $Q' = 0$

$4x - 3x^2 = 0$

$x(4 - 3x) = 0$

$x = 0$ or $4 = 3x \Rightarrow x = \frac{4}{3}$

we need positive #'s, so $x \neq 0$

thus $x = \frac{4}{3}$

$y = 2 - x = 2 - \frac{4}{3} = \frac{2}{3}$

12. Volume open rectangular box w/ square base.

$V = x^2 h = 32 \text{ ft}^3 \Rightarrow h = \frac{32}{x^2}$

$SA = x^2 + 4xh \leftarrow \text{minimal}$

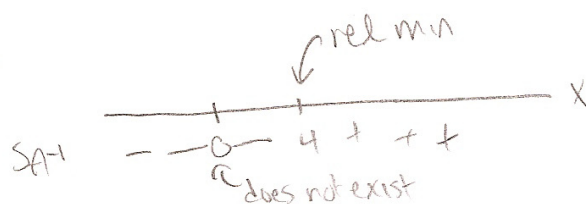
$SA = x^2 + 4x \left(\frac{32}{x^2} \right) = x^2 + 128x^{-1}$ (note $x \neq 0$)

$SA^{-1} = 2x - \frac{128}{x^2}$ set $SA^{-1} = 0$

$0 = 2x - \frac{128}{x^2}$

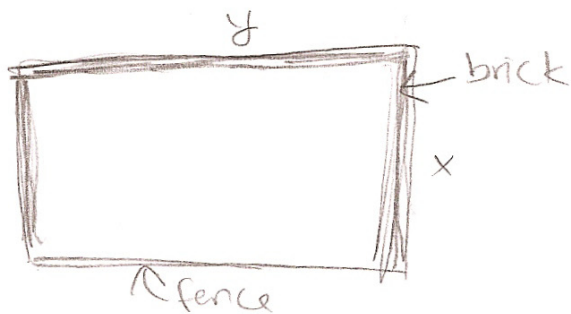
$\frac{128}{x^2} = 2x \Rightarrow 64 = x^3 \Rightarrow x = 4 \Rightarrow h = \frac{32}{(4)^2} = 2$

confirm:



$$5. A = 75 \text{ ft}^2 = xy$$

$$C = 5y + 3(10)x \\ = 5y + 30x$$



$$y = \frac{75}{x}$$

$$C = 5\left(\frac{75}{x}\right) + 30x = \frac{375}{x} + 30x = 375x^{-1} + 30x \quad \text{note 416}$$

$$C' = -\frac{375}{x^2} + 30$$

$$\text{set } C' = 0$$

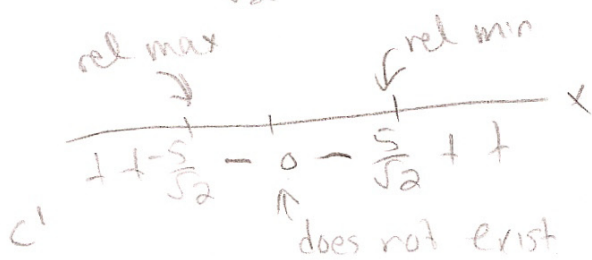
$$\frac{375}{x^2} = 30 \Rightarrow x^2 = 12.5 = \frac{25}{2} \Rightarrow x = \pm \frac{5}{\sqrt{2}}$$

we can ignore $x \leq 0$, so $x = \frac{5}{\sqrt{2}}$

$$y = \frac{75}{x} = 15\sqrt{2}$$

answer: $\frac{5}{\sqrt{2}} \times 15\sqrt{2}$ feet

confirm it's a min:



2.6 1. (A) Avg amount of cherries = 90 cherries

(2)

(B) Max amount: 180 cherries

(C) # of orders: 6 orders

(D) Pounds sold in 1 year: 1080 lbs

(2) (A) $I = C + O = 7(90) + 6(50) = \930

(B) $I = C + O = 7(90)(2) + 6(50) = \1560

(4) (A) $I = 160r + 32\left(\frac{x}{2}\right) = 160r + 16x$

(B) $rx = 640$

(C) $r = \frac{640}{x}$

$$I = 160\left(\frac{640}{x}\right) + 16x = 102400x^{-1} + 16x$$

$$I' = -\frac{102400}{x^2} + 16 \quad x \neq 0$$

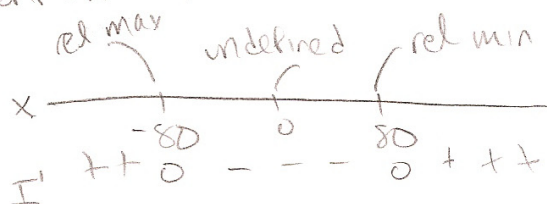
$$\text{Set } I' = 0$$

$$16 = \frac{102400}{x^2} \Rightarrow x^2 = 6400 \Rightarrow x = \pm 80 \quad \text{choose } \boxed{x=80}$$

$$r = \frac{640}{80} = \boxed{8}$$

$$I_{\min} = 160(8) + 32\left(\frac{80}{2}\right) = \$2560$$

confirm min



28.

$$xy = 50 \text{ in}^2$$

$$x = \frac{50}{y}$$

$$P = (x+2)(y+1)$$

$$P = xy + 2y + x + 2$$

$$= 52 + 2y + \frac{50}{y}$$

$$P' = 2 - \frac{50}{y^2}$$

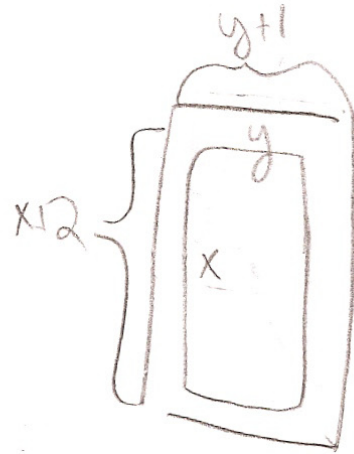
$$y \neq 0$$

$$\text{set } P' = 0$$

$$\frac{50}{y^2} = 2 \Rightarrow y = \pm 5 \text{ in.}$$

$$\text{ignore } y \leq 0, \text{ so } y = 5 \text{ in.} \rightarrow x = \frac{50}{5} = 10 \text{ in}$$

confirm min:

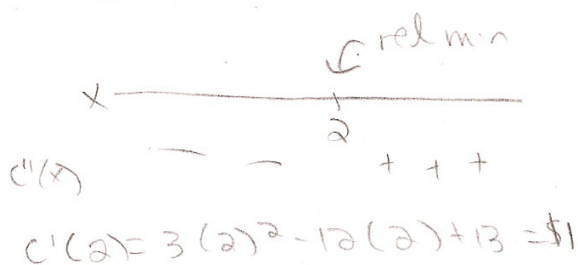


- 28 $f(x)$ is defined for all $0 \leq x \leq 5$
 $f'(x) < 0$ for all x

$f(x)$ will have its greatest value at $x=0$, since $f'(x) < 0$ implies that the value is decreasing for all x .

Section 2.7

- ① $C(x) = x^3 - 6x^2 + 13x + 15$
 marginal cost: $C'(x) = 3x^2 - 12x + 13$
 $C''(x) = 6x - 12$
 set $C''(x) = 0$
 $6x - 12 = 0 \Rightarrow x = 2$

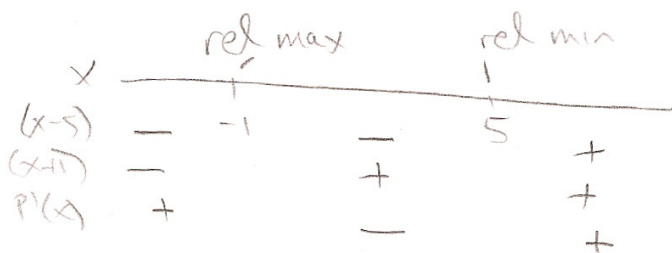


- ⑤ $C(x) = x^3 - 6x^2 + 13x + 15$
 $R(x) = 20x$
 $P(x) = R(x) - C(x) = -x^3 + 6x^2 + 13x - 15$
 $P'(x) = -3x^2 + 12x + 15$
 set $P'(x) = 0$

$$0 = -3x^2 + 12x + 15$$

$$0 = -3(x^2 - 4x - 5) = -3(x-5)(x+1)$$

$x = 5$ or $x = -1$ we need $x \geq 0 \Rightarrow x = \5



(12) (x, p) : x = people p = price

$(4000, \$50)$ $(3800, \$52)$

$$p - 50 = \frac{52 - 50}{3800 - 4000} (x - 4000)$$

$$p - 50 = \frac{-2}{200} (x - 4000)$$

$$p - 50 = \frac{-x}{100} + 4$$

$$p = \frac{-x}{100} + 54$$

$$R(x) = x \cdot p = x \left(\frac{-x}{100} + 54 \right) = \frac{-x^2}{100} + 54x$$

$$R'(x) = \frac{-x}{50} + 54$$

$$\text{set } R'(x) = 0$$

$$\frac{x}{50} = 54 \Rightarrow x = 2700$$

$$p(2700) = \frac{-2700}{100} + 54 = \boxed{\$27}$$