Math 122 Fall 2008

Quiz #2

Questions 1-4 are all long-response questions. In each case, be careful to indicate your final answer and show how you obtained it. Answers with no supporting work will get no credit.

You may assume the following trigonometric identities on this quiz.

(a)
$$\sin^2(x) + \cos^2(x) = 1$$

(b)
$$\tan^2(x) + 1 = \sec^2(x)$$

(c)
$$\sin^2(x) = \frac{1}{2}(1 - \cos(2x))$$

(d)
$$\cos^2(x) = \frac{1}{2}(1 + \cos(2x))$$

You may assume the following integral formulas on this quiz.

(a)
$$\int \tan(x) dx = \ln(|\sec(x)|) + C$$

(b)
$$\int \sec(x)dx = \ln(|\sec(x) + \tan(x)|) + C$$

You should not use your calculator for any of the problems on this quiz.

1. (2 points) Evaluate the following indefinite integral to find the most general antiderivative.

$$\int \frac{\sin(x) + 2}{\cos(x)} dx.$$

2. (3 points) Evaluate the following indefinite integral to find the most general antiderivative. $\int \tan^5(x) dx.$

3. (3 points) Evaluate the following indefinite integral to find the most general antiderivative.

$$\int x\sqrt{1-x^4}\,dx\,.$$

4. (2 points) Evaluate the following indefinite integral to find the most general antiderivative.

$$\int \frac{1}{x\sqrt{x^2+9}} dx.$$