Solving a Catering Problem with the Greedy Set Cover Algorithm AJ Druck, Neha Gupta, Olivia Montanha, Juliette Wong

Introduction
× The Cheesecake Factory

- Clients supply:
- Number of attendees (20)
- Dietary restrictions of attendees
- Minimum number of dishes they want - 2 appetizers, 4 main dishes, 2 desserts

Goal: choose set of dishes that

- Maximizes expected revenue
- Meets dietary restrictions of all attendees


## Dała (Ałtendees)

Note: we created this data based on the percentages for these food allergies in the United States

| $\times$ | $0->$ none |
| :--- | :--- |
| $\times$ | 1 -> vegetarian |
| $\times$ | $2->$ vegan |
| $\times$ | $3->$ lactose intolerant |
| $\times$ | $4->$ seafood free |
| $\times$ | 5 -> nut allergy |
| $\times$ | $6->$ gluten free |
| $\times$ | $7->$ no meat or dairy |
| $\times$ | $8->$ gluten free vegetarian |

(8/20-40\%)
× 1 ->vegetarian
(2/20-10\%)
× 2 -> vegan
(1/20-5\%)
x 3 -> lactose intolerant
$\times 4$-> seafood free
(4/20-20\%)
$\times 5$-> nut allergy
$\times 6$-> gluten free
(1/20-5\%)
$\times \quad 7->$ no meat or dairy
8 -> gluten free vegetarian
(1/20-5\%)
(1/20-5\%)
(1/20-5\%)
(1/20-5\%)


| Dietary Restrictions | Gluten Free | Meat Free | Dairy Free | Nut Free | Seafood Free | Egg Free |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: |
| 0 None | $\square$ | $\square$ | $\square$ | $\square$ | $\square$ | $\square$ |
| 1 Vegetarian | $\square$ | $\checkmark$ | $\square$ | $\square$ | $\checkmark$ | $\square$ |
| 1 Vegetarian | $\square$ | $\checkmark$ | $\square$ | $\square$ | $\checkmark$ | $\square$ |
| 2 Vegan | $\square$ | $\checkmark$ | $\square$ | $\square$ | $\square$ | $\square$ |
| 3 Lactose Intolerant | $\square$ | $\square$ | $\square$ | $\square$ | $\square$ | $\square$ |

## Dała (Food)

$X$
Based on our encoding of attendees, we represented each dish on the menu as a set of types of individuals who could consume that food


|  | Price | Gluten Free | Meat Free | Dairy Free | Nut Free | Seafood Free | Egg Free |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Parmesan Garlic Cheese Bread | 8.95 | $\square$ | $\checkmark$ | $\square$ | $\square$ | $\checkmark$ | $\square$ | $\{0,1,4\}$ |
| Roadside Sliders | 9.95 | $\square$ | $\square$ | $\square$ | $\checkmark$ | $\checkmark$ | $\checkmark$ | $\{0,4,5\}$ |
| Chicken Pot Stickers | 10.95 | $\square$ | $\square$ | $\square$ | $\checkmark$ | $\checkmark$ | $\square$ | $\{0,4,5\}$ |
| Avocado Eggrolls | 11.5 | $\square$ | $\checkmark$ | $\checkmark$ | $\square$ | $\checkmark$ | $\square$ | $\{0,1,4\}$ |
| Quesadilla | 9.95 | $\square$ | $\checkmark$ | $\square$ | $\checkmark$ | $\checkmark$ | $\checkmark$ | $\{0,1,4,5\}$ |
| Fried Mac and Cheese | 11.5 |  | $\checkmark$ |  | $\checkmark$ | $\checkmark$ | $\square$ | $\{0,1,4,5\}$ |
| Southern Fried Chicken Sliders | 10.95 | $\square$ | $\square$ | $\square$ | $\checkmark$ | $\checkmark$ | $\square$ | $\{0,4,5\}$ |
| Hot Spinach and Cheese Dip | 10.95 | $\square$ | $\checkmark$ | $\square$ | $\checkmark$ | $\checkmark$ | $\square$ | $\{0,1,4,5\}$ |
| Tex Mex Eggrolls | 10.95 | $\square$ | $\square$ | $\square$ | $\checkmark$ | $\checkmark$ | $\square$ | $\{0,4,5\}$ |
| Fried Calamari | 12.95 | $\square$ |  | $\square$ | $\checkmark$ | $\square$ | $\square$ | $\{0,5\}$ |
| Buffalo Blasts | 11.95 | $\square$ | $\square$ | $\square$ | $\checkmark$ | $\checkmark$ | $\square$ | $\{0,4,5\}$ |
| Sweet Corn Tamale Cakes | 10.95 | $\checkmark$ | $\checkmark$ | $\square$ | $\checkmark$ | $\checkmark$ | $\checkmark$ | $\{0,1,4,5,6,8\}$ |

## Set Cover Algorithm

x Have a universe

- In our case it would be a set of the types of people present: $\{0,1,2,3,4,5,6,7,8\}$
$\times \quad$ Have a set of subsets whose union equals the universe
- Would be the dishes
- Ex. $\{\{0\},\{0,1,2,3,4,7\},\{0,5,6\},\{0,1,5,6,8\}\}$
$\times$ Find the smallest set of subsets whose union equals the universe
- i.e. find the smallest number of dishes that satisfies everyone (and maximises revenue)


## Algorithm

## × Greedy Set Cover Algorithm

```
def set_cover(universe, subsets, weights):
    """Find a family of subsets that covers the universal set"""
    elements = set(e for s in subsets.values() for e in s)
    # Check the subsets cover the universe
    if elements != universe:
                return None
```

    covered \(=\operatorname{set}()\)
    cover = []
    \# Greedily add the subsets with the most uncovered points
    while covered != elements:
        subset, bestI = maxHelper(subsets, covered, weights)
        del subsets[bestI]
    
covered $=\operatorname{set}()$
cover = []
\# Greedily add the subsets with the most uncovered points while covered != elements:
subset, bestI = maxHelper(subsets, covered, weights)
del subsets[bestI] del weights[bestI]
cover.append((subset, bestI))
covered |= subset
return cover

Agorithm (cont.)
def maxHelper(subsets, covered, weights):
$\operatorname{maxS}=$ None
$\operatorname{maxH}=-1$
bestI = None
for key in subsets:
heuristic $=$ len(subsets[key]-covered)*weights[key] if maxS == None or heuristic > maxH:
$\operatorname{maxS}=$ subsets[key]
maxH = heuristic bestI = key
return maxS, bestI

Results

Appetizers:
× Factory Chopped Salad -- \$12.50

* Guacamole Made-To-Order -- \$11.95
* Factory Nachos -- \$12.50

Results (cont.)
Main Dishes:
× Chinese Chicken Salad -- \$14.95
× Cobb Salad -- \$14.95
× Sante Fe Salad -- \$15.50
$\times$ Four Cheese Pasta -- \$15.95
× Luau Salad -- \$14.95

* Evelyn's Favorite Pasta -- \$15.95



Results (cont.)

Desserts:
× Bowl of Fresh Strawberries -- \$7.50
x Dairy-Free Key Lime Pie -- \$7.95
× Godiva Chocolate Cheesecake -- \$7.95


## Results (cont)

$\times$ We assumed that of the foods an individual can consume, they have an equal chance of choosing each dish
E [Appetizers] = \$245.97
E [Main Dishes] = \$305.81
E [Dessert] = \$155.40

## Total Expected Revenue: \$707.18

Expected Revenue/Person: \$35.36

## Conclusion

x Compared to a visual inspection of the data, the algorithm chose the correct dishes
$\times$ This specific example can be generalized to different menus, number of attendees, number of dietary restrictions, number of dishes requested, etc.

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