

21-301 Combinatorics
Homework 5
Due: Monday, October 26

1. Prove that if u, v are the only vertices of odd degree in a graph G , then there is a path from u to v in G .
2. Let $G = (V, E)$ be a graph with minimum degree at least three. Show that it contains a cycle of even length. (Hint: Consider a longest path).
3. Prove that if T_1, T_2, \dots, T_k are pair-wise intersecting sub-trees of a tree T , then T has a vertex common to T_1, T_2, \dots, T_k . (Hint: use induction on k).