## 21-301 Combinatorics

Homework 10
Due: Wednesday, December 2


1. How many ways are there of $k$-coloring the squares of the above cross if the group acting is $e_{0}, e_{1}, e_{2}, e_{3}$ where $e_{j}$ is rotation by $2 \pi j / 4$. Assume that instead of 15 squares there are $4 n+1$.
2. How many ways are there of $k$-coloring the squares of the same cross if the group acting is $e_{0}, e_{1}, e_{2}, e_{3}, p, q, r, s$ where $p, q, r, s$ are horizontal, vertical, diagonal reflections.
3. How many ways are there of $k$-coloring the 7 vertices of the tree below if the group acting is has elements $e, g_{a}, g_{b}, g_{c}$ where $e$ is the identity and $g_{x}$ rigidly rotates the tree below $x$.

