

# Homework 7

## June 17

1. 5.1.36 (Hint: this has essentially nothing to do with norms).

We didn't have time to discuss the idea of normalizing in class, so we will do a few problems to practice the idea. Do the following series of problems:

2. Prove that if  $S = \{\mathbf{v}_1, \dots, \mathbf{v}_k\}$  is an orthogonal set and  $c$  is a nonzero scalar then  $S = \{\mathbf{v}_1, \dots, c\mathbf{v}_i, \dots, \mathbf{v}_k\}$  is a set of orthogonal set.

The process of normalization is to change a orthogonal set  $S = \{\mathbf{v}_1, \dots, \mathbf{v}_k\}$  into an orthonormal set  $S' = \{\mathbf{v}'_1, \dots, \mathbf{v}'_k\}$  where the  $\mathbf{v}'_i$  are nonzero if  $\mathbf{v}_i$  is, each of the  $\mathbf{v}'_i$  are unit vectors, and  $\{\mathbf{v}_i, \mathbf{v}'_i\}$  are linearly dependent (i.e. one is a multiple of the other). The process is done by iterating the theorem in part *a*. Look at Example 5.6 in the book for an example to follow.

3. 5.1.11 and 5.1.12 to normalize those orthogonal sets (unless they already are orthogonal).

## June 18

4. 5.1.17
5. 5.1.26
6. 5.2.14

## June 19

7. 5.3.6
8. 5.3.10
9. 5.3.12 (I didn't do an example like this, but it follows example 5.14 in the text)