

1. Write the line $\mathbf{r}(t) = 4\mathbf{i} - 2\mathbf{k} + t(-\mathbf{i} + 3\mathbf{j} + \mathbf{k})$ in parametric and symmetric form.

Determine whether each pair of lines intersects. If so, find the point of intersection and the angle formed by the lines.

2. $\mathbf{r}_1(t) = 2\mathbf{i} - \mathbf{j} + t(\mathbf{j} - \mathbf{k})$
 $\mathbf{r}_2(t) = 3\mathbf{i} + \mathbf{j} - \mathbf{k} + t(\mathbf{i} + \mathbf{k})$

3. $\mathbf{r}_1(t) = \mathbf{i} + \mathbf{j} + \mathbf{k} + t(2\mathbf{i})$
 $\mathbf{r}_2(t) = 4\mathbf{j} - \mathbf{k} + t(-\mathbf{i} + \mathbf{j})$

4. Find the distance from the point $P(1, 1, 1)$ to the line, ℓ defined by $x = 2$, $y = t$, $z = 1 - t$

5. Find the equation of the plane orthogonal to $\langle 3, 1, -4 \rangle$ and containing the point $P(3, 0, 9)$

6. A plane is given by the equation $3x + y - 2z = 4$. What vector is normal to this plane? Name any three points contained in this plane.

7. Consider the line ℓ given by $x = -2t + 1$, $y = t - 3$, $z = -t + 5$. The goal of this problem is to find a coinciding line, m where the equation for x is $x = u$.
- What is the direction vector of ℓ ?
 - What is the x component in the direction vector of m ?
 - What is the whole direction vector of m ?
 - Let P be the point used to specify m . What is the x coordinate of P ?
 - Since P is on m , it is also on ℓ . Use this fact to find all three coordinates of P .
 - What are the parametric equations of m ?
 - Verify your answer by finding two points that are contained in both ℓ and m .

Determine whether the following planes are identical, parallel, or intersecting. If intersecting, find the line where it intersects. (Hint: Since the line lies on both planes, it will be normal to both normal vectors. To find a point, guess one coordinate and solve for the other two.)

8. $x + y + z = 0$
 $3x + 2y + z = 3$

9. $2x + 6y - 6z = 2$
 $\frac{x-1}{3} + y - z = 0$

10. $2x - y + 8z = 10$
 $-4x + 2y - 16z = 10$