

**Essential Uses of Probability in Analysis**  
**Part II. Domains with moving boundaries.**  
**The heat equation and reflected Brownian motion**

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