## Homework Set 6

1) A group is simple if it has no nontrivial proper normal subgroups. Let $G$ be a simple group of order 168. How many elements of order 7 are there in $G$ ?

2 Let $G$ be a group of order 231. Prove that the (unique) Sylow 11-subgroup of $G$ is in the center.
3) Prove that for every even integer $p \geq 2$, there exists a constant $c(p)$ such that any one-distance set with respect to the $L_{p}$-norm in $R^{n}$ has at most $n^{c(p)}$ points.
4) Let $\lambda$ be a nonzero integer, $J$ be the $m \times m$ all ones matrix, and $D$ be the $m \times m$ diagonal matrix with positive integer diagonal entries $\gamma_{1}, \ldots, \gamma_{m}$. Compute the determinant of $A=\lambda J+D$.

