

**Department of Mathematical Sciences**  
**Carnegie Mellon University**  
21-393 Operations Research II  
Test 2

Name: \_\_\_\_\_

Problem	Points	Score
1	35	
2	35	
3	30	
Total	100	

**Q1: (35pts)**

Use the KKT conditions to solve

Minimise  $(x_1 - 2)^2 + (x_2 - 2)^2$  subject to  $x_1 + x_2 \leq 2, x_1 + 3x_2 \leq 5$ .

**Q2: (35pts)**

Formulate the following as an integer program:

The Financial Aids office at Carnegie Mellon University is preparing its awards for the coming year. It has selected  $n$  students to receive awards, and wants to grant at least  $m_i$  dollars to Student  $i$ ,  $i = 1, 2, \dots, n$ . The office has  $s$  different scholarships available; Scholarship  $j$  confers the amount  $a_j$  on its recipient. The office may have to award several scholarships to an individual in order to provide the minimum it has decided that he/she will receive. The office cannot however reduce the amount of a scholarship award. If the office does not award a particular scholarship then it becomes available for next year. The office wishes to maximise the amount of money not spent in this way.

**Q3: (30pts)**

In an inventory system for a single product there is a fixed cost of  $A$  for making an order. No stockouts are allowed. The inventory cost per period is  $Ih^{1/2}$  where  $h$  is the average amount of stock held. determine an optimal purchasing/stock strategy.